

# GTL Geometry Template Library

-for stl-like polygon manipulation

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# Overview

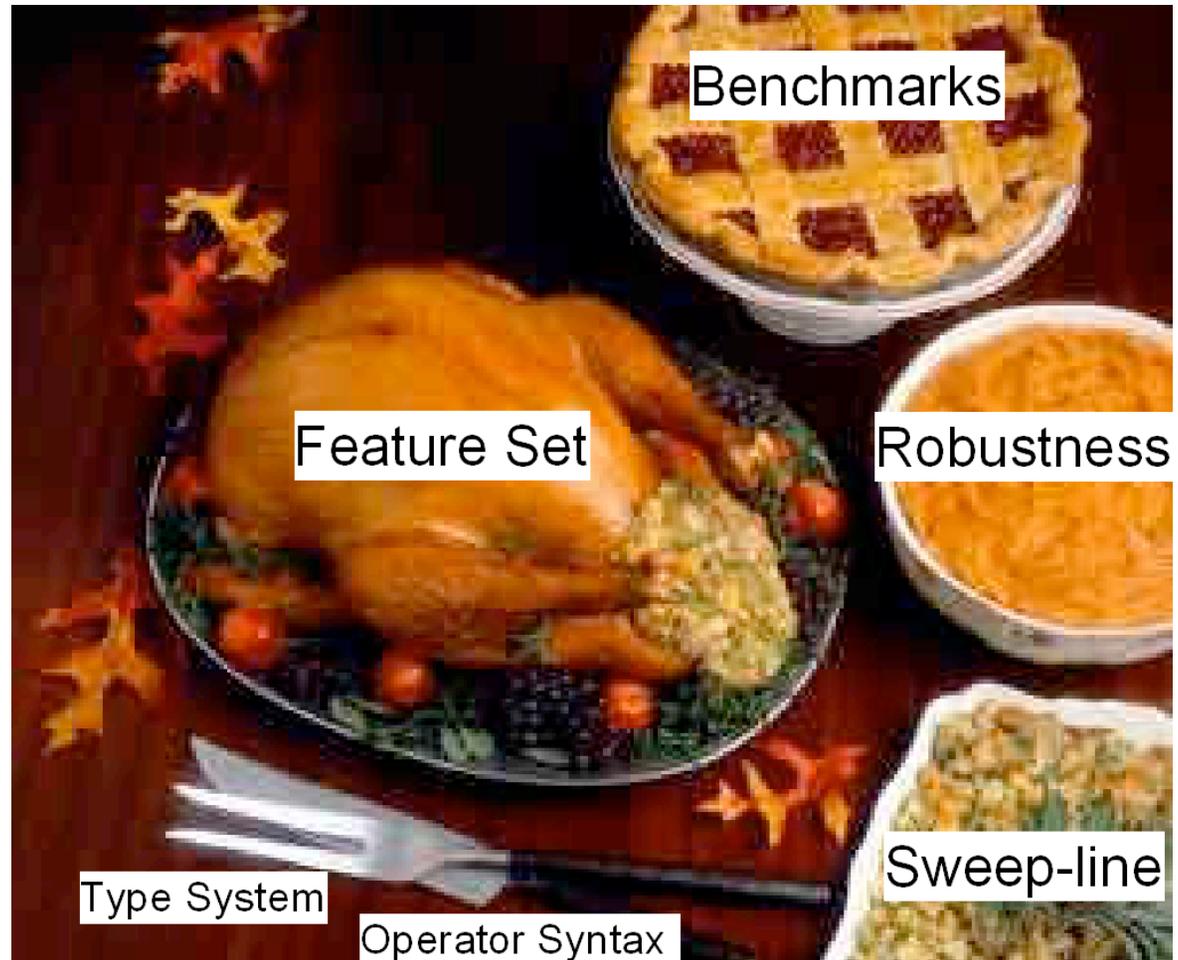
- Intel badly needed high performance algorithms for planar polygon manipulation
  - I implemented them
- We have 2D Cartesian geometry
  - Coordinate, Interval, Point, Rectangle, Polygon, Polygon Set
  - Library of concepts for each
- Many generic functions that operate on conceptual types
  - API strives for symmetry, consistency and simplicity
- Some pretty heavy weight algorithms under the hood
- 3 man years and 30kloc

# Introduction

- Implemented goofy template argument inheritance type system and Manhattan geometry features
- Request for interest from boost in 2007
  - Discussed the design on boost dev list
  - Found out the design was bad and needed to be redone the boost way
    - Thank you Joel Guzman
- Added 45 degree geometry features
- After six months of work we got permission from Intel to release under boost license
  - Discussed the code on the boost dev list
  - Got a lot of feedback on specific design considerations
- Rewrote the interfaces to be more generic by using tag dispatching
  - Got more feedback on design considerations from boost, especially refinement
- Re-rewrote the interfaces to be more generic still and based on SFINAE
- Added arbitrary-angle geometry features
  - Got feedback on arbitrary-angle algorithms and robustness considerations from boost
    - Thank you Fernando Cacciola
- Ported new SFINAE interfaces to MSVC9
  - Thank you Steven Watanabe
- The library now looks more like Joel said it should back in 2007
  - We may pursue formal review this year
- Deployed library to internal users who are using it now to create the next generation of silicon fabrication process technology and microprocessors

# Agenda

- GTL Feature Set
- Benchmark Comparisons
- Generic Sweep-line Booleans Algorithm
- Numerical Robustness
- Geometry Concepts Type System
- Booleans Operator Syntax



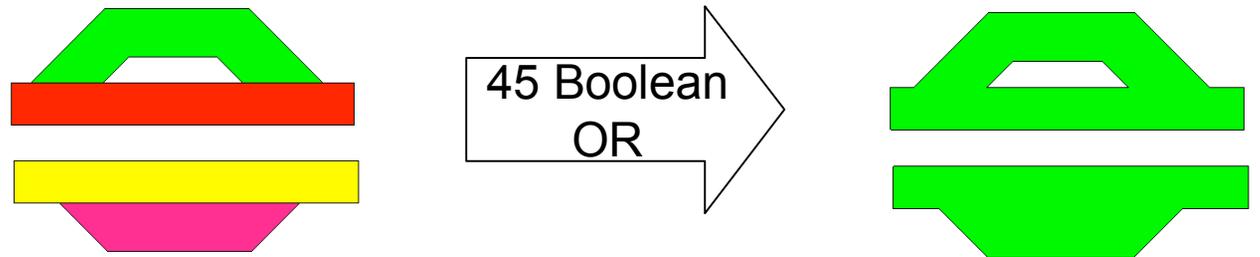
# Primary GTL Feature

- Boolean operations on sets of polygons

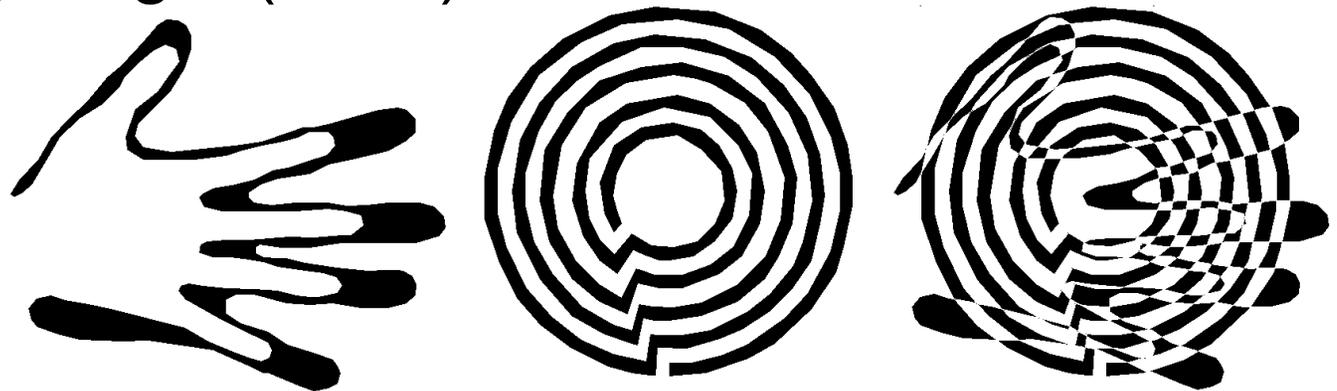
– Manhattan



– 45-degree



– Arbitrary Angle (XOR)



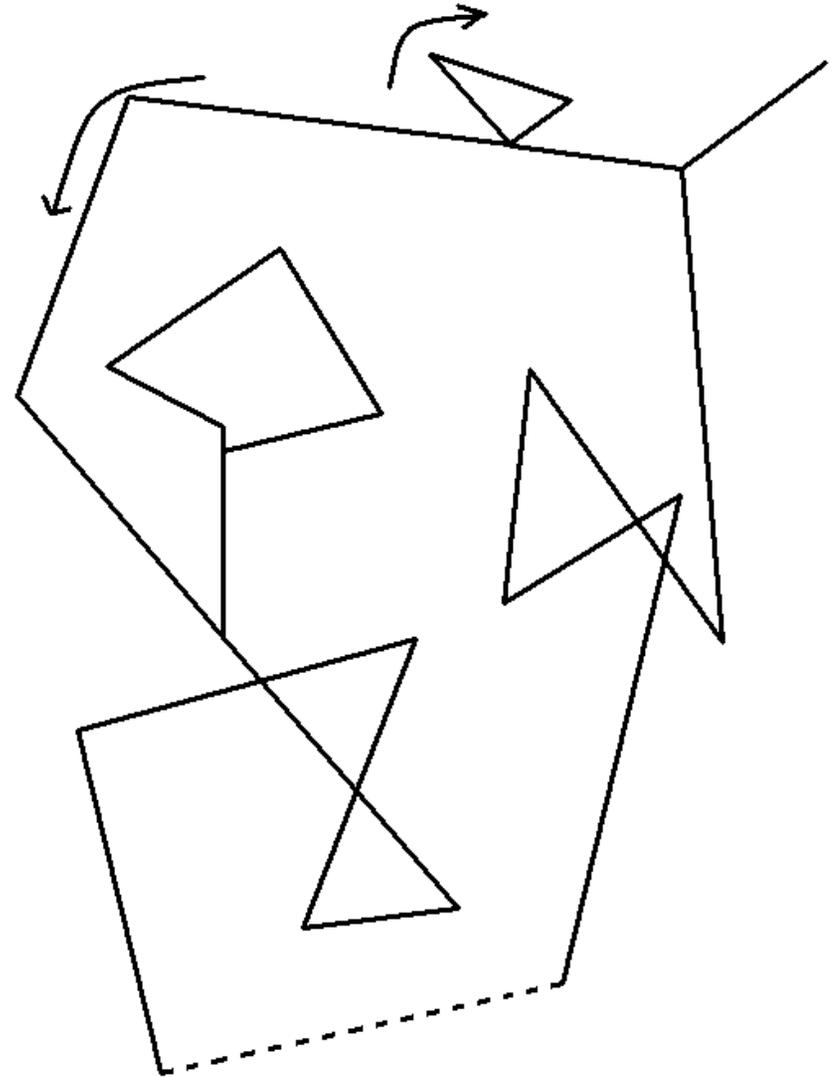
# Using Booleans

```
void clip_and_subtract(polygon_set& d,  
                      polygon a, polygon b, rectangle c) {  
    d = (a & c) - b;  
}
```

- Productive operator syntax
- Clip polygon a against bounding box c, then subtract polygon b, storing the result in polygon set d
- Takes longer to say than to type
- No try/catch and no memory management

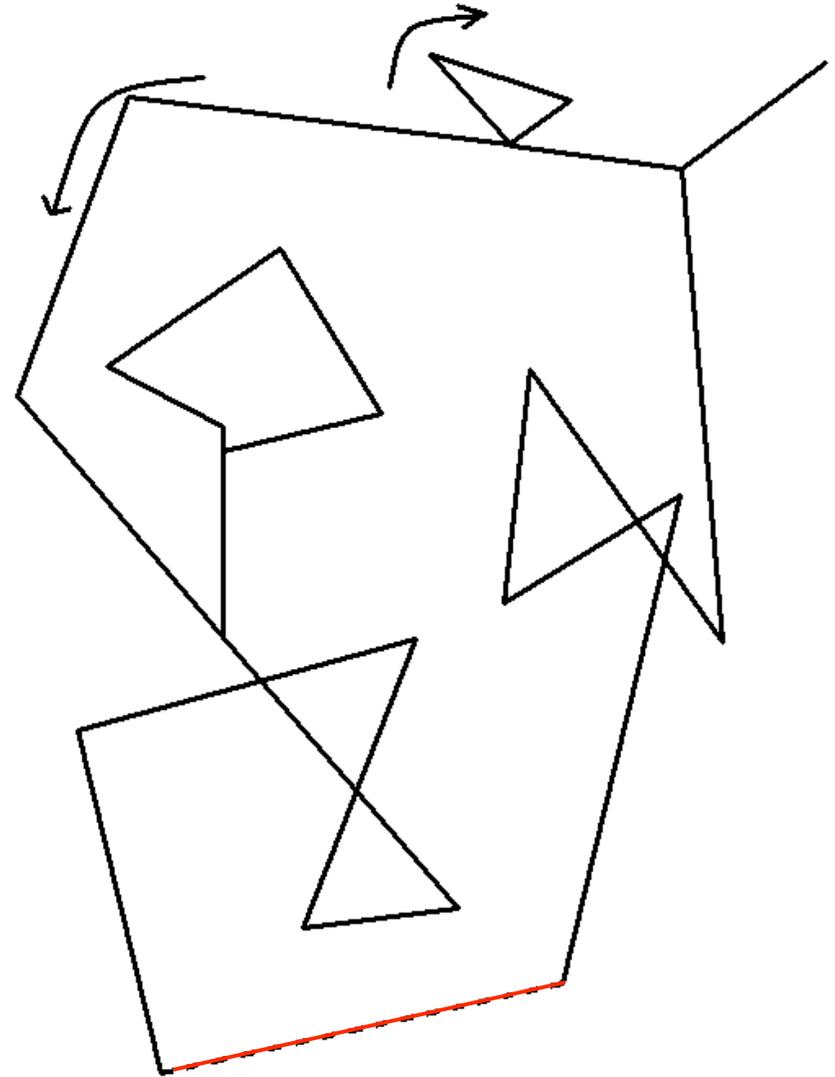
# Details Of Booleans

- No preconditions placed on input polygons



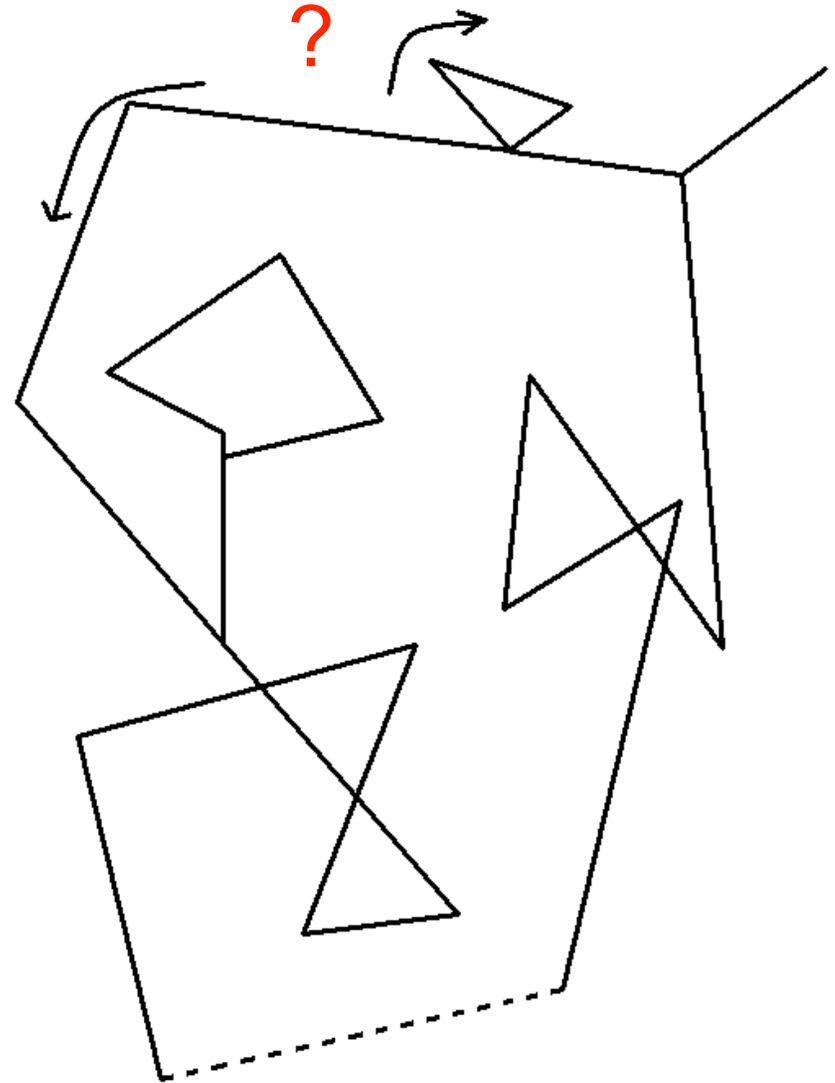
# Details Of Booleans

- No preconditions placed on input polygons
  - Open/closed semantic for last vertex



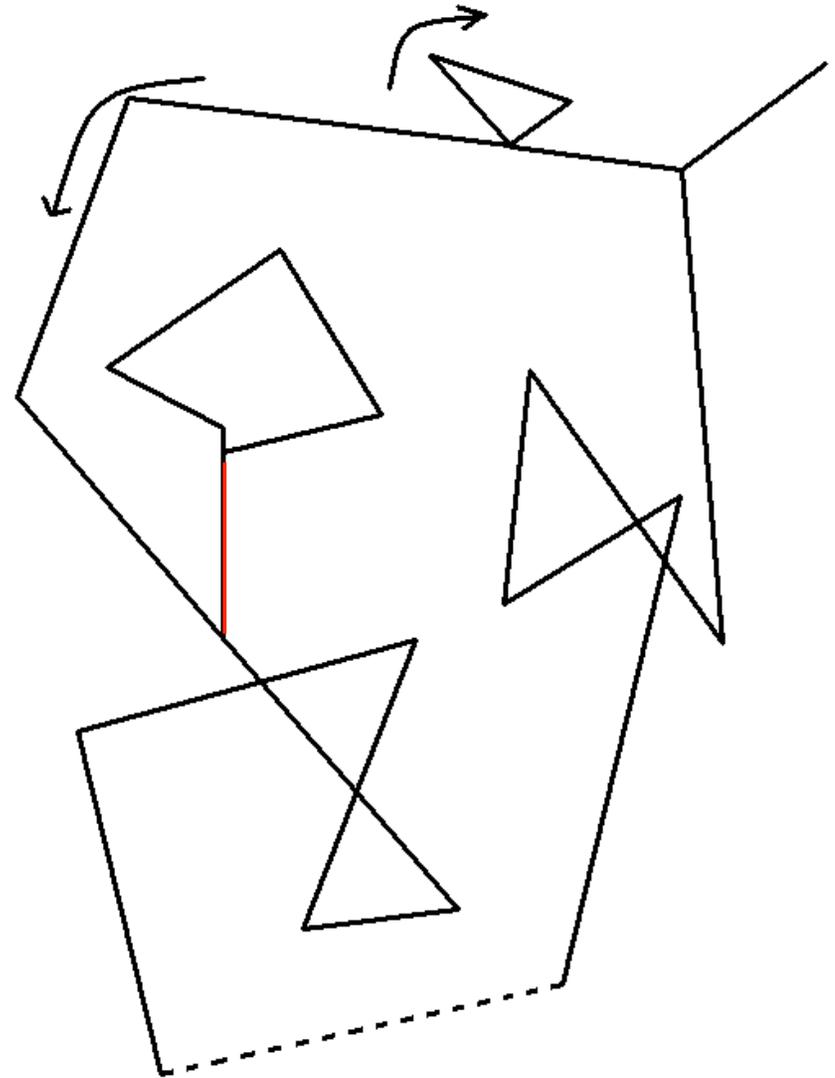
# Details Of Booleans

- No preconditions placed on input polygons
  - Open/closed semantic for last vertex
  - Winding direction conventions not enforced



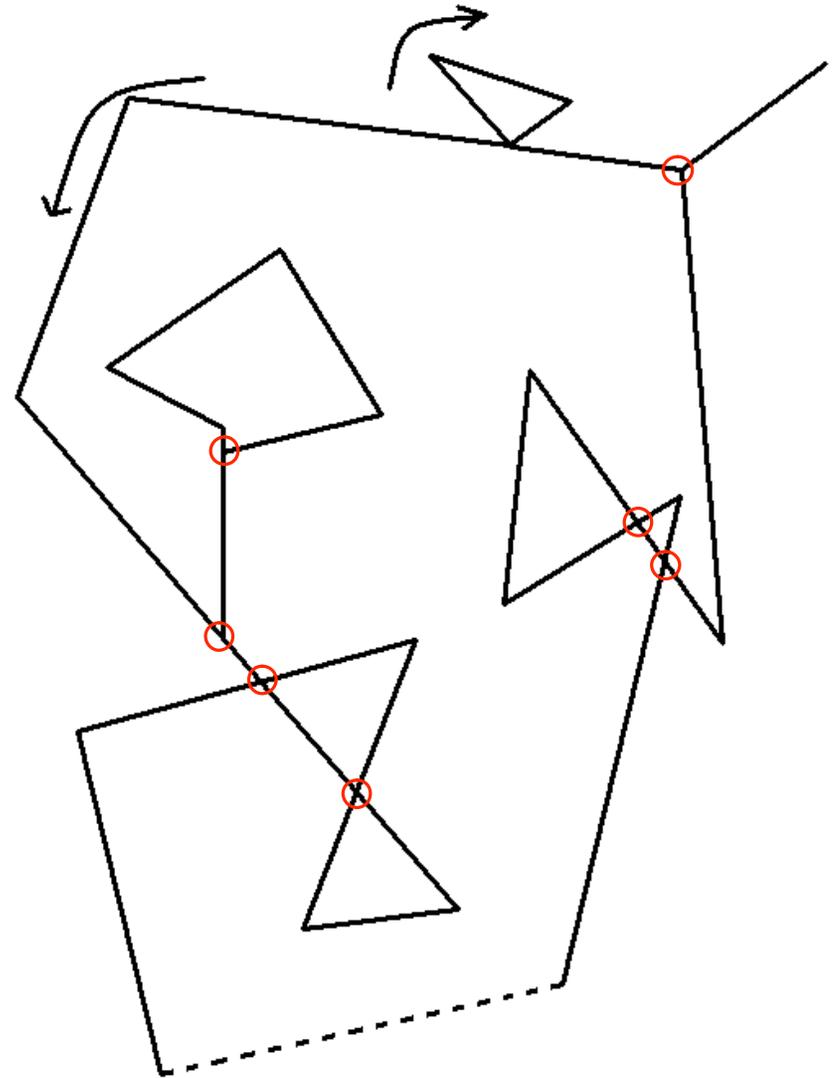
# Details Of Booleans

- No preconditions placed on input polygons
  - Open/closed semantic for last vertex
  - Winding direction conventions not enforced
  - Input polygons may be
    - self touching



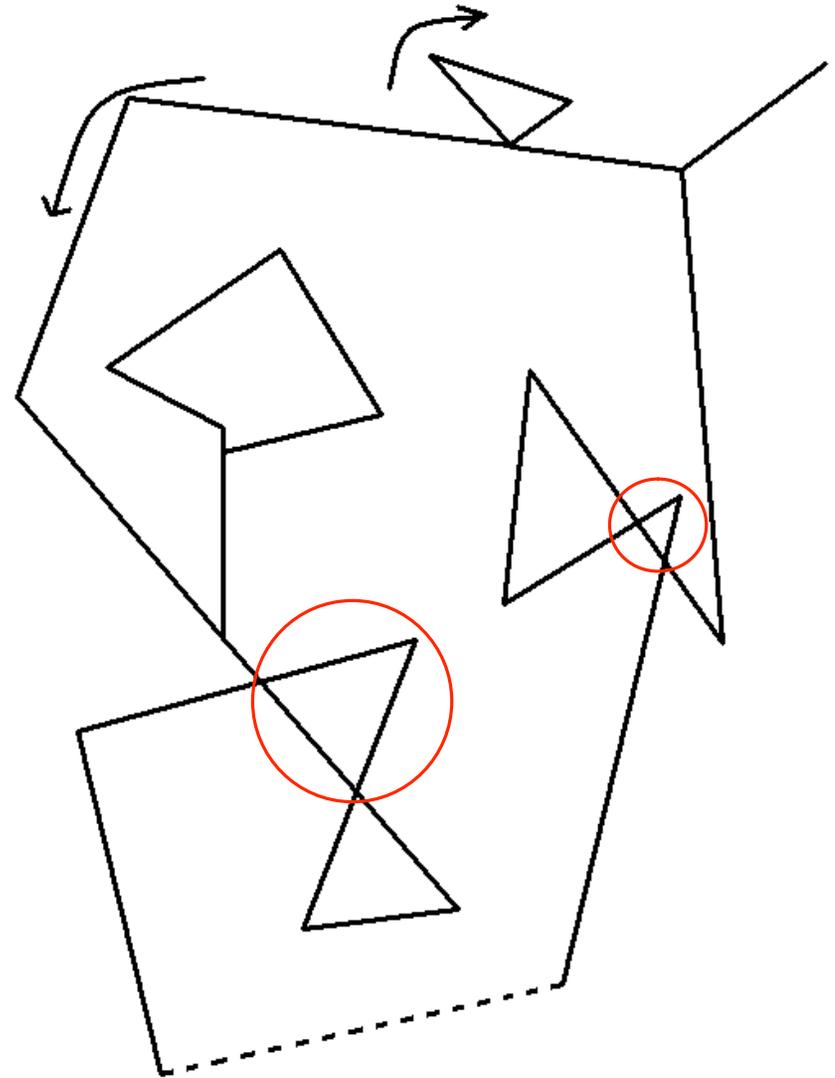
# Details Of Booleans

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  - Winding direction conventions not enforced
  - Input polygons may be
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    - self intersecting



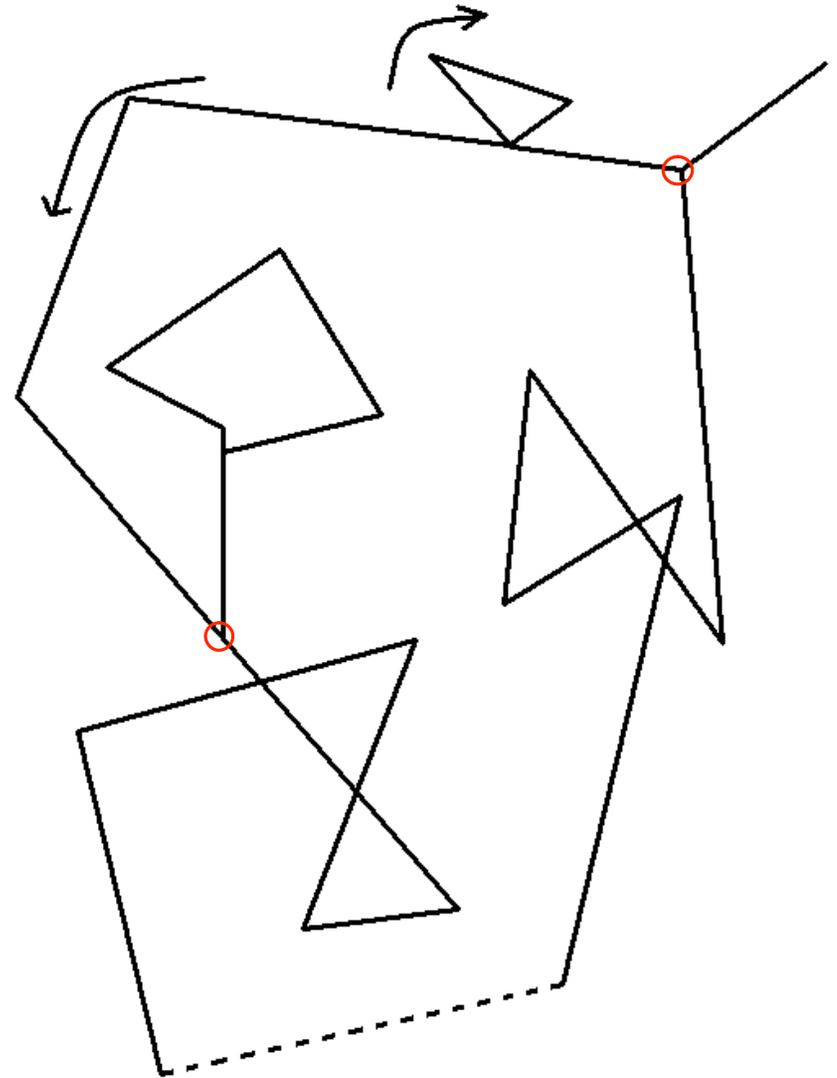
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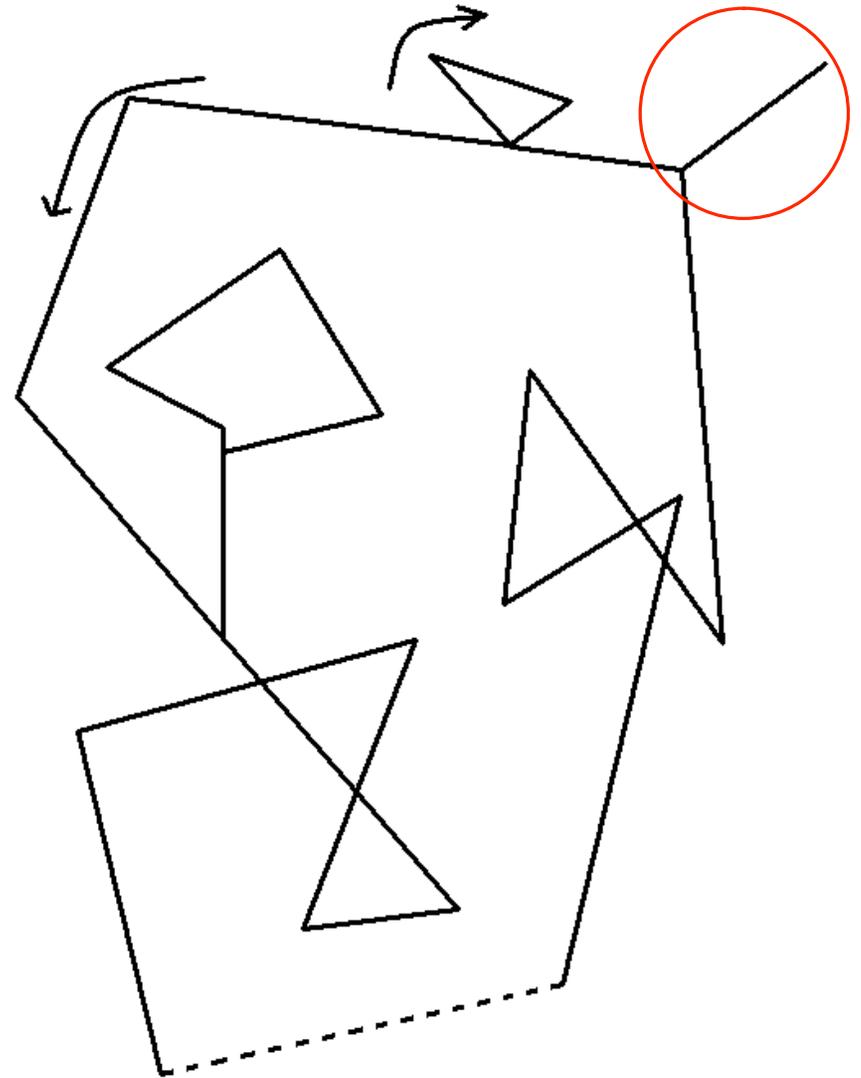
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- No preconditions placed on input polygons
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    - self overlapping
  - Correctly handles duplicate/co-linear points



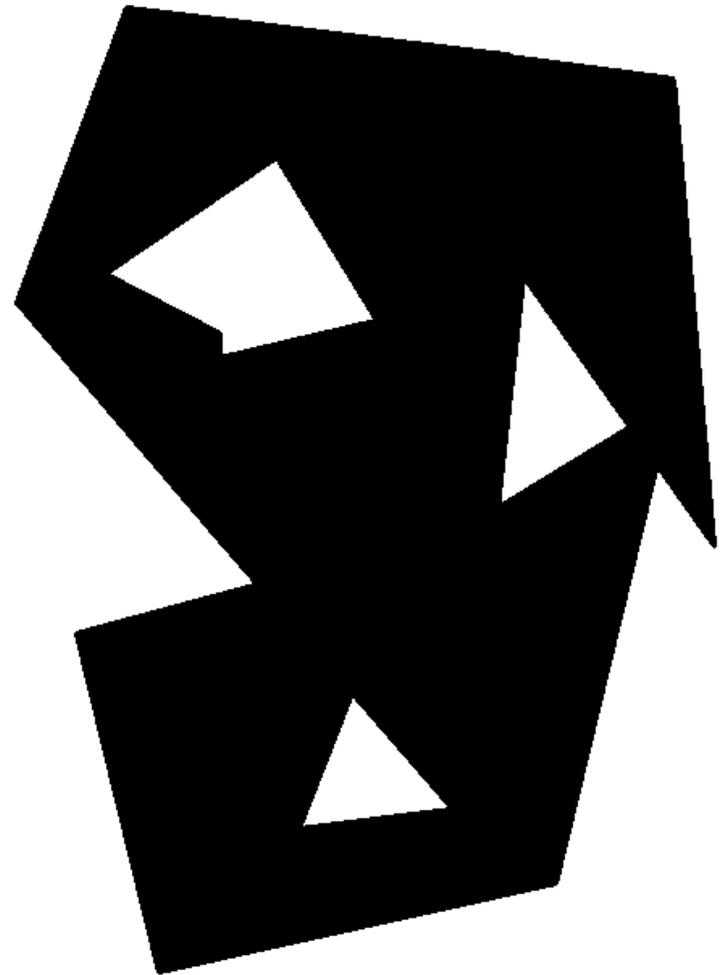
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  - Correctly handles zero degree angles and polygons that degenerate to lines and points



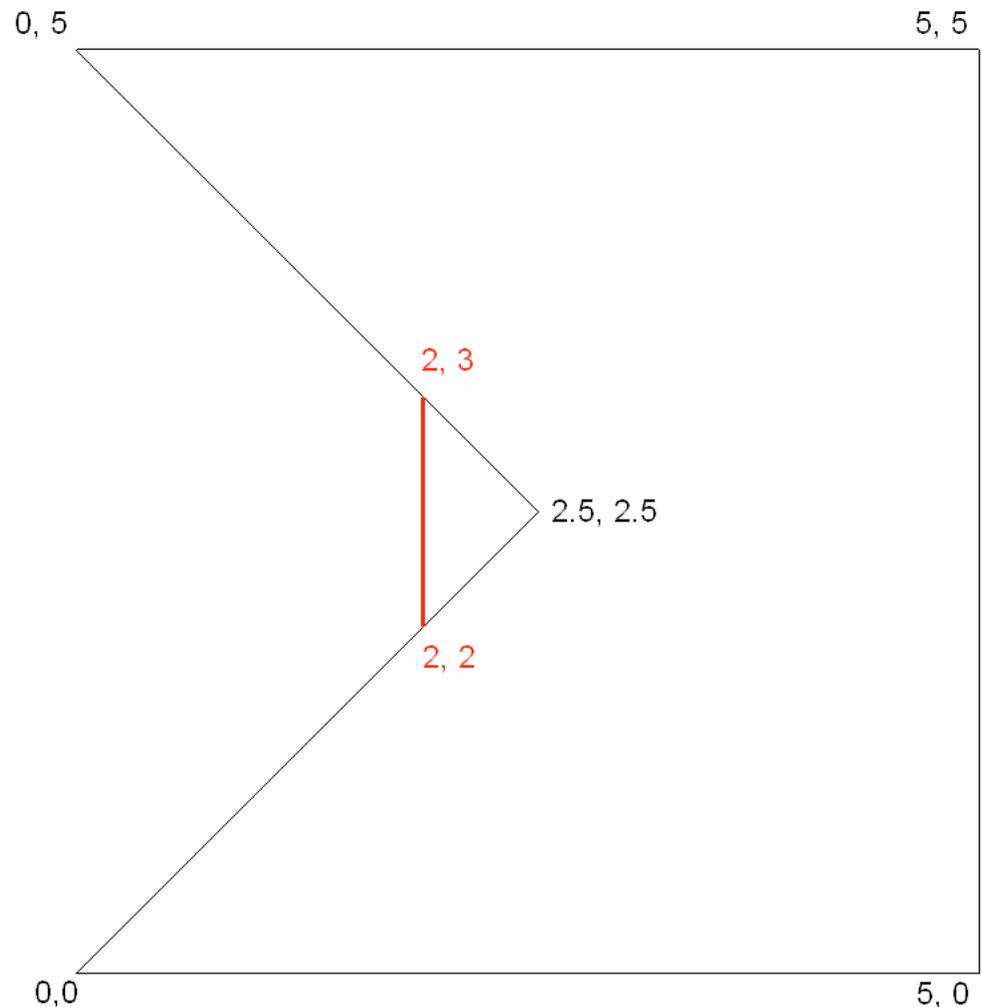
# Details Of Booleans

- No preconditions placed on input polygons
  - Open/closed semantic for last vertex
  - Winding direction conventions not enforced
  - Input polygons may be
    - self touching
    - self intersecting
    - self overlapping
  - Correctly handles duplicate/co-linear points
  - Correctly handles zero degree angles and polygons that degenerate to lines and points
  - To produce a clean result



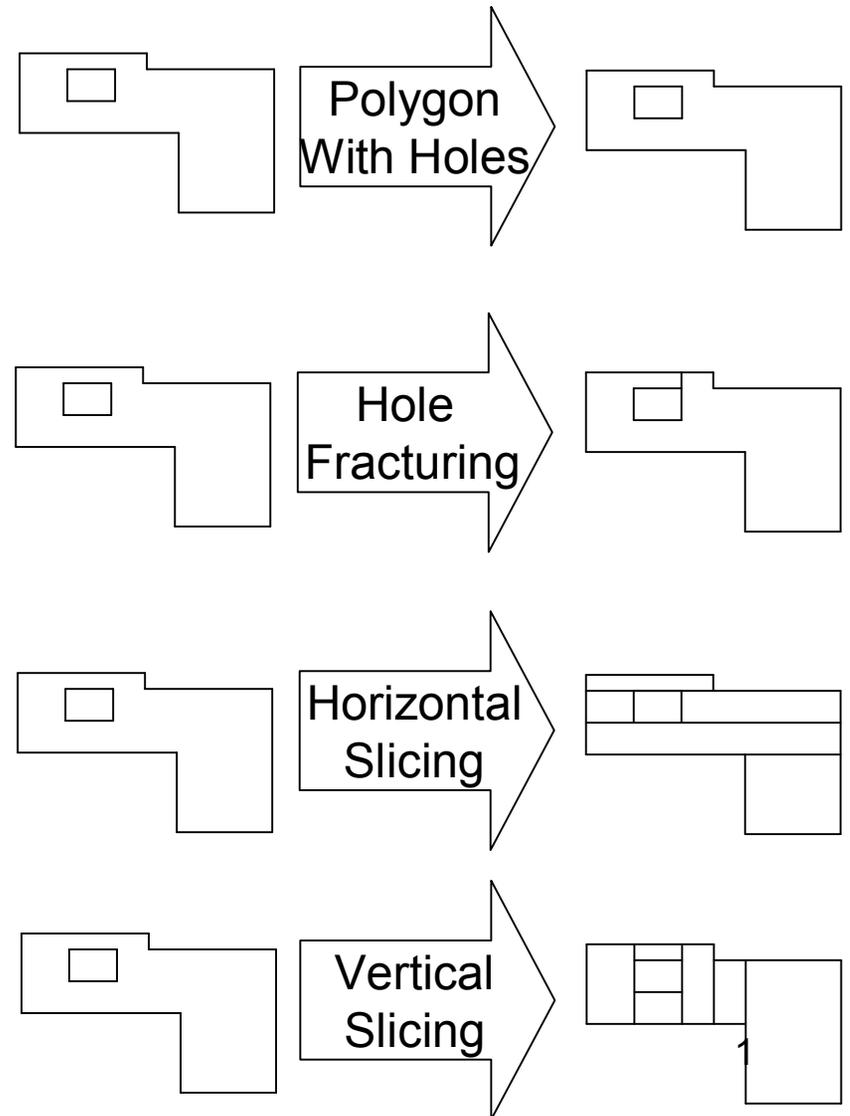
# Details of 45-degree Booleans

- Preserve 45-degree nature of geometry at output
- Handle off-grid intersections by inserting an edge to approximate the output region



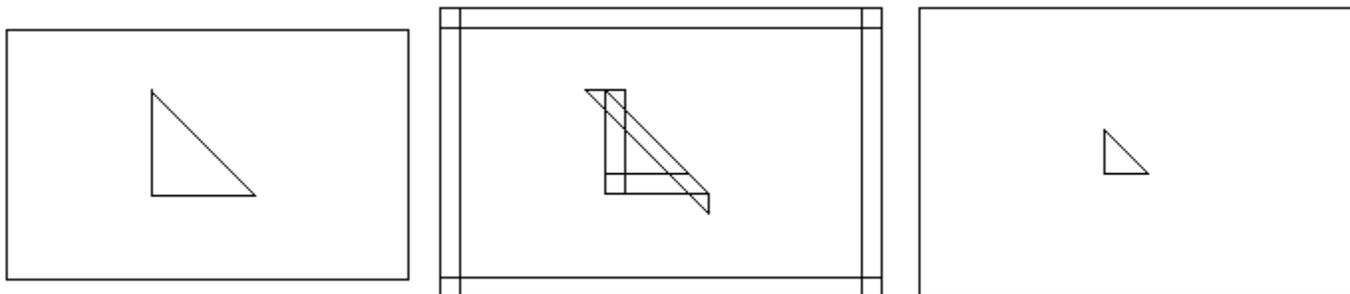
# Boolean Operation Output Modes

- **Manhattan Booleans**
  - Polygons with lists of holes
  - Keyhole holes to outer polygon
  - Horizontal and vertical sliced rectangle tiling
- **45-degree Booleans**
  - Polygon with lists of holes
  - Keyhole holes to outer polygon
  - Vertical sliced trapezoid tiling
- **Arbitrary-angle Booleans**
  - Polygon with lists of holes
  - Keyhole holes to outer polygon



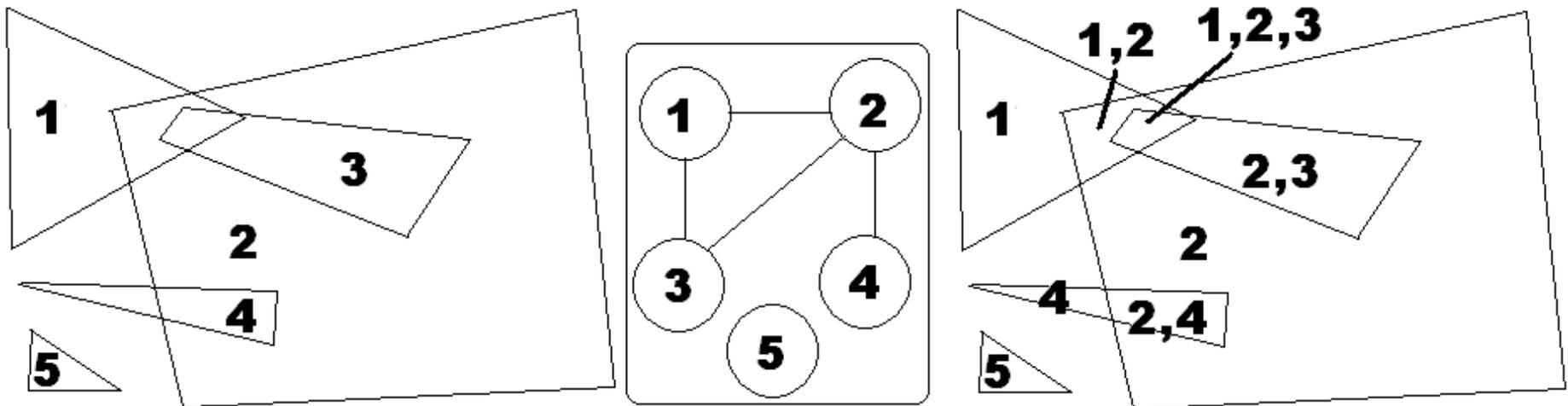
# Polygon Buffering/Resizing/Offsetting

- Manhattan
  - Uniform resizing
  - Resizing by different amount in each of the four directions
  - Optionally leave corners unfilled
- 45-Degree
  - Uniform resizing
  - Preserve original topology or cut off acute angled corners at resizing distance
  - Snapping options for moving 45-degree edges

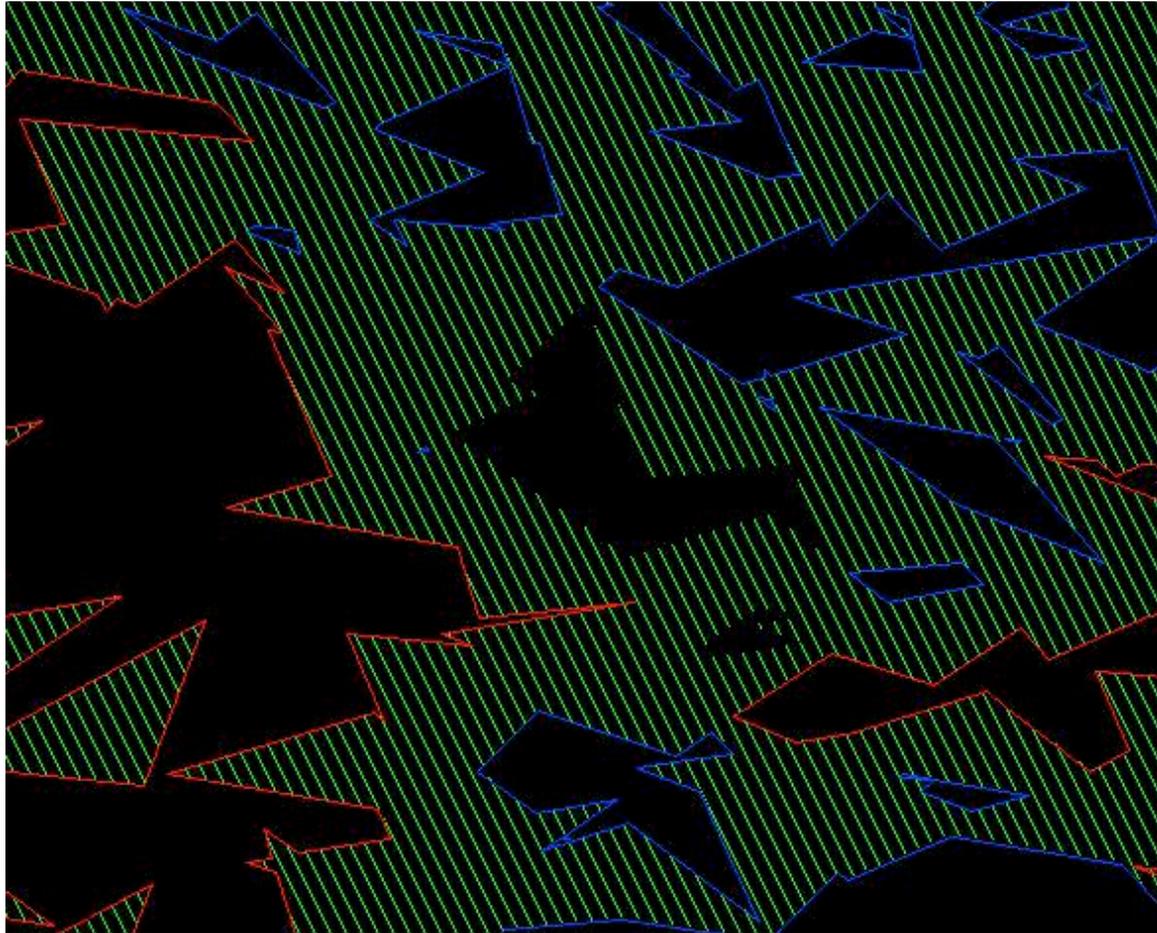


# Many More Features

- Rectangle query tree
- Maximum enclosed rectangle in Manhattan polygon
- Connectivity Extraction
- Property Merge/Map Overlay
- Etc.

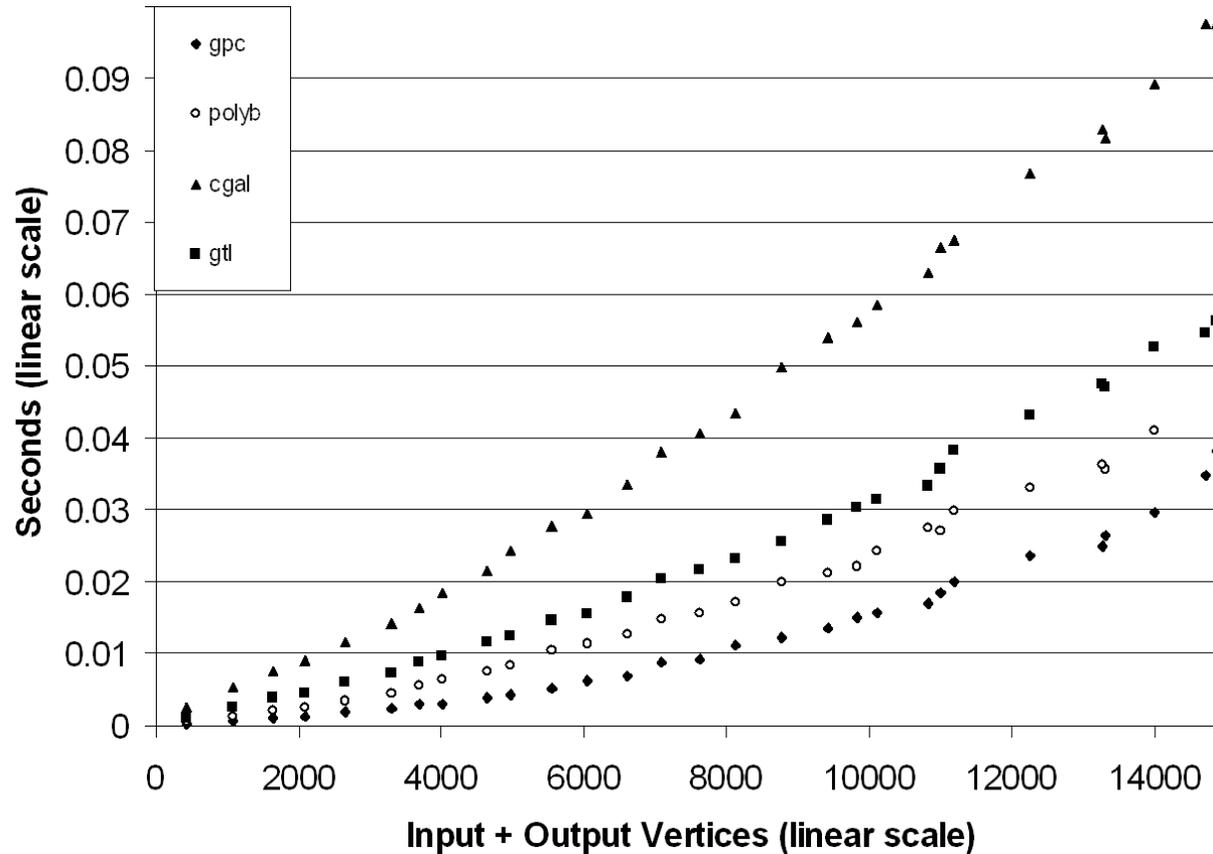


# Small Arbitrary-angle Input Benchmark Comparison



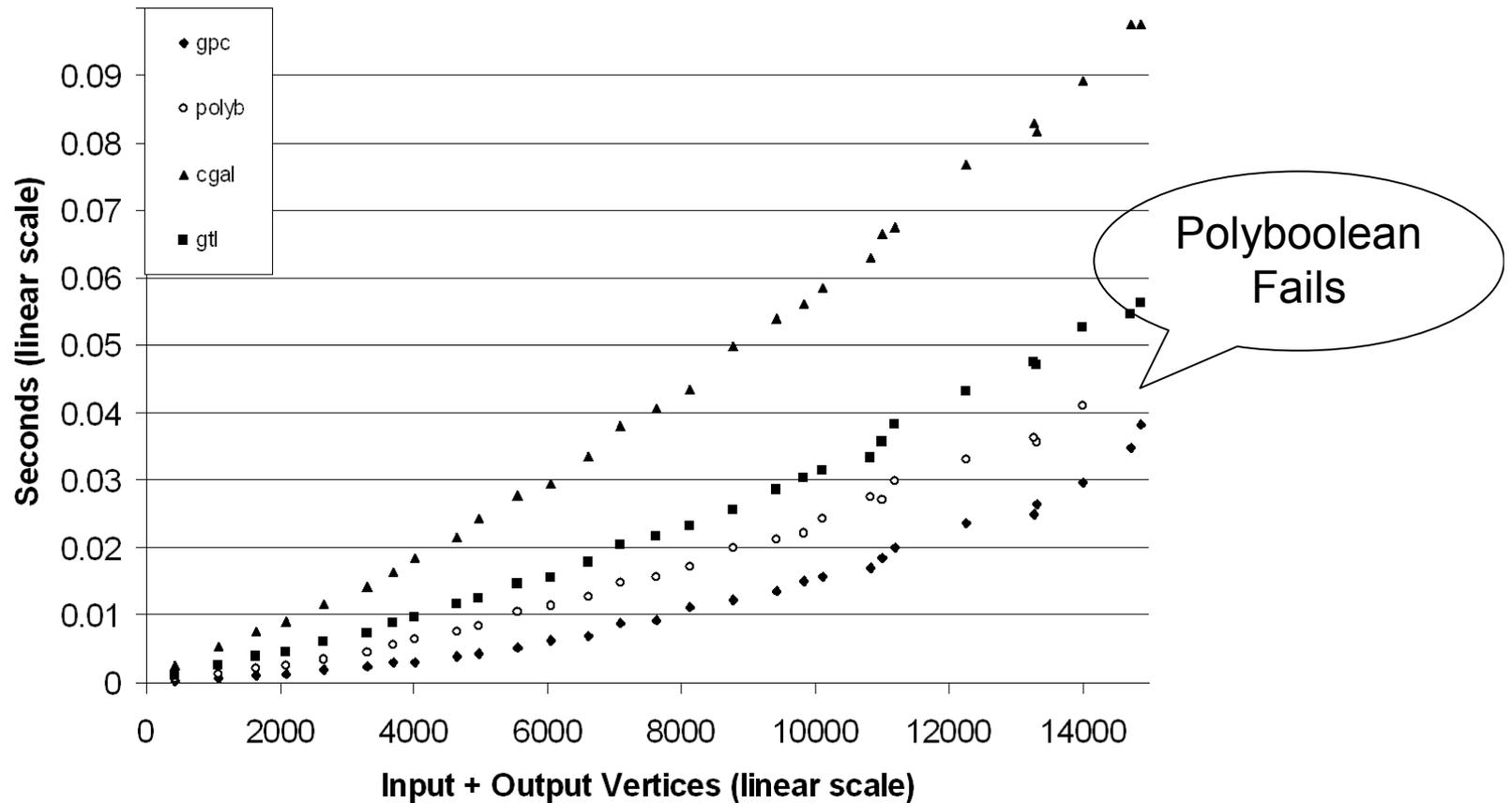
- Runtime for intersection operation

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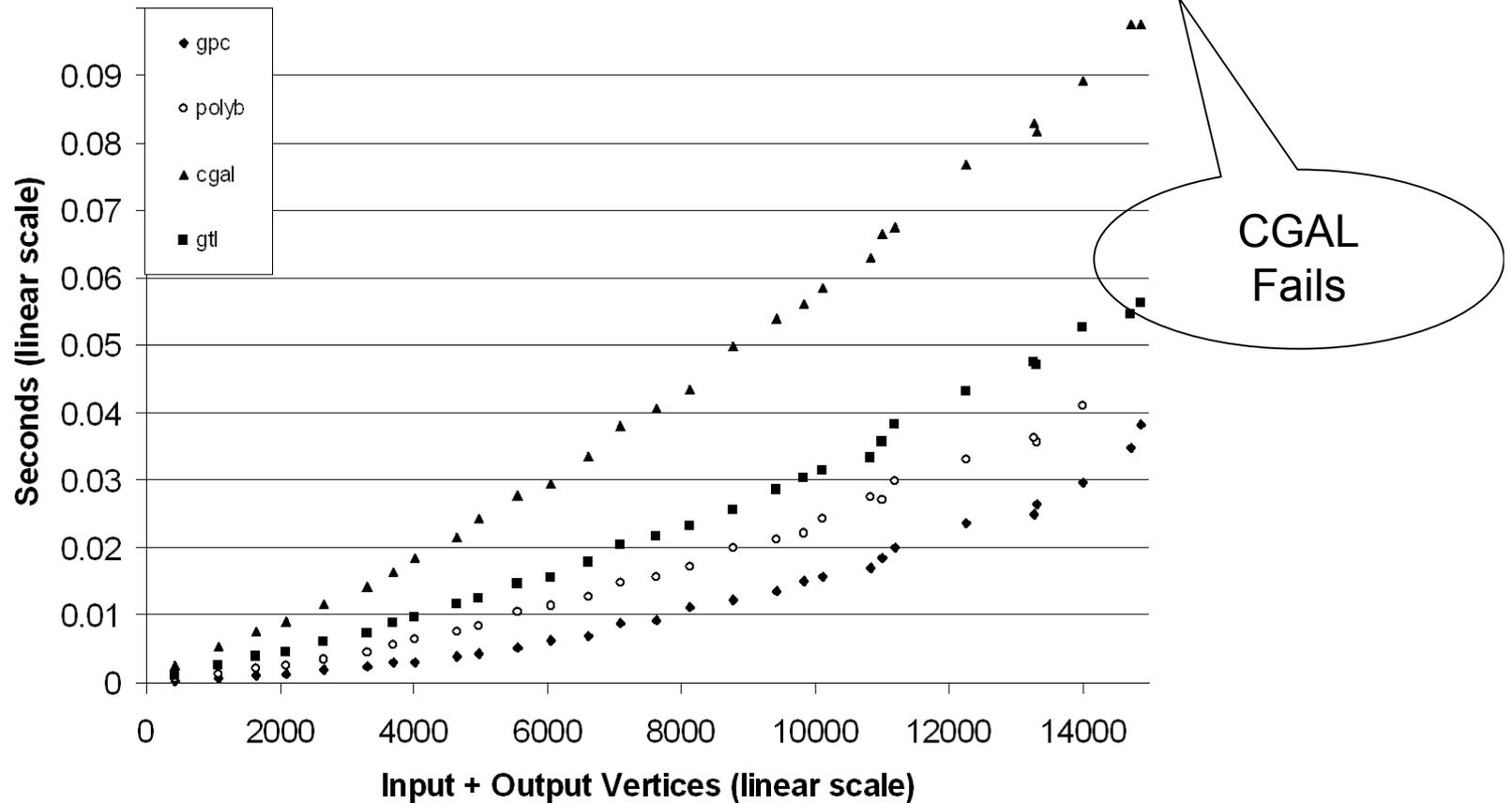
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# Small Arbitrary-angle Input Benchmark Comparison



- Runtime for intersection operation

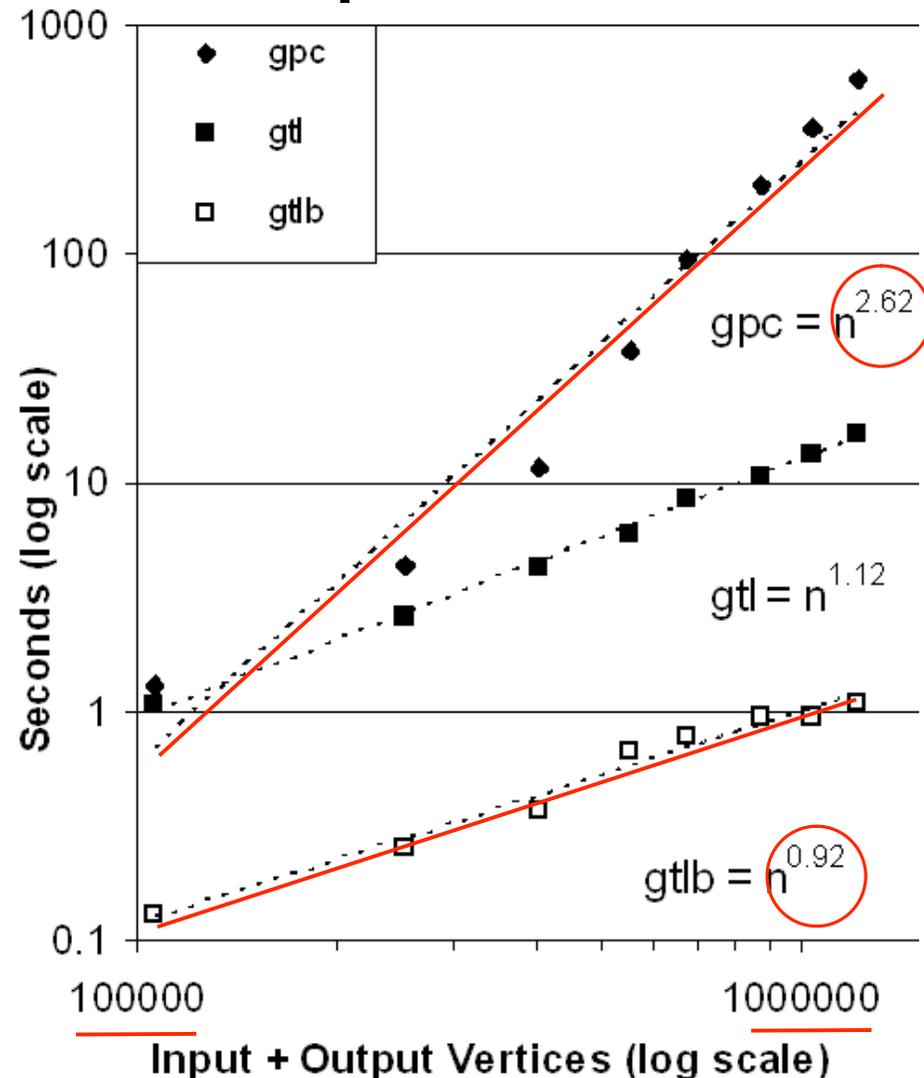
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- Runtime for intersection operation

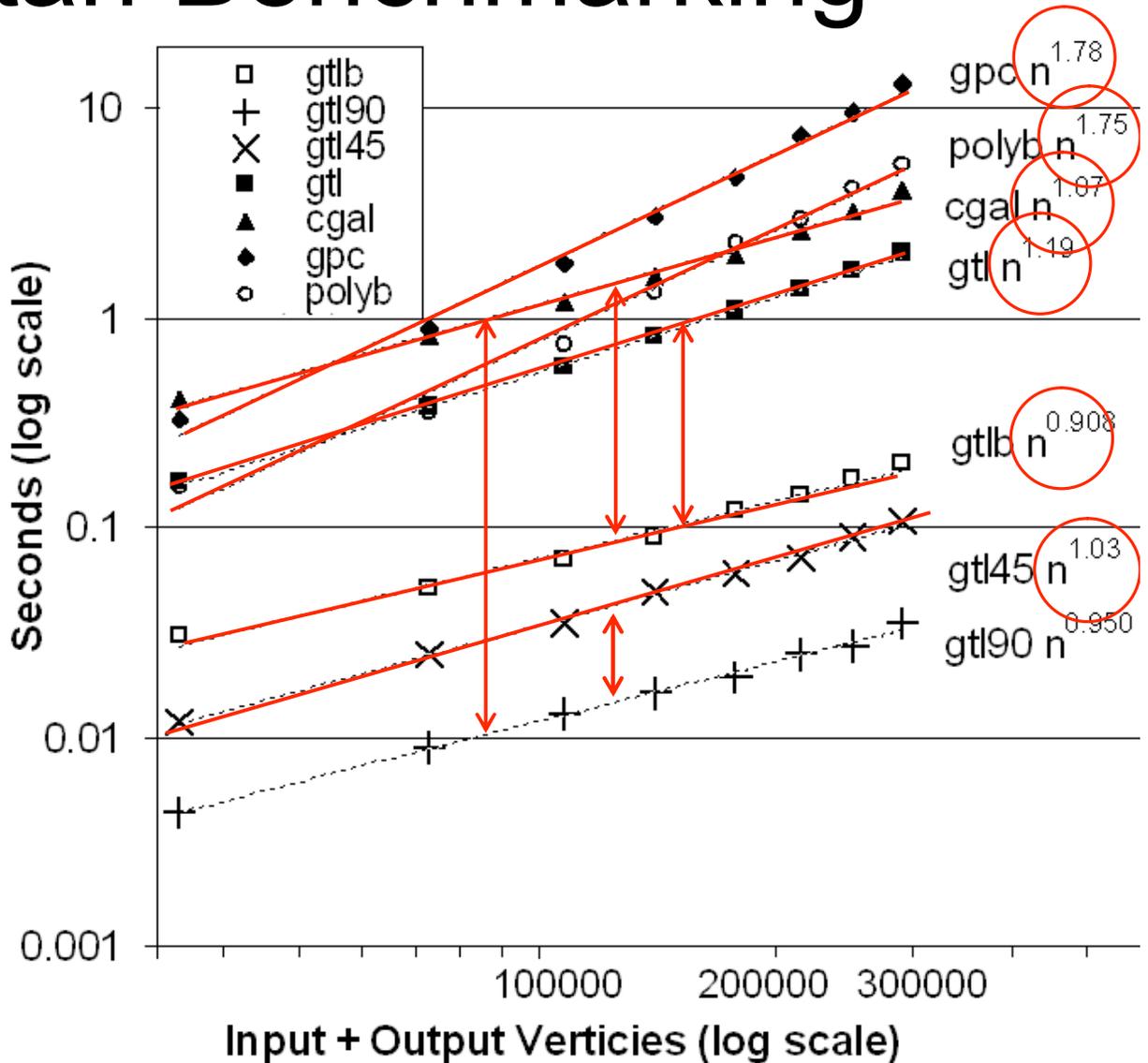
# Large Scale Arbitrary-angle Performance Comparison

- One to two orders of magnitude larger than previous benchmark
- Though fastest for small inputs, GPC does not scale well
- gtlb excludes line segment intersection
- Core Boolean is  $n \log n$ , Intel micro-architecture accelerates processing of large vectors



# Manhattan Benchmarking

- 100X performance delta between optimal gtl 90-degree algorithm and general algorithms
- gtl 45-degree Boolean is optimal
- Core arbitrary angle Boolean (gtlb) is optimal
- gtl arbitrary angle Boolean is slightly suboptimal due to line segment intersection
- CGAL is optimal, but has a high constant factor
- GPC and PolyBoolean both scale sub-optimally
- Optimal is:  
near linear  $O(n \log n)$   
runtime



# Benchmarking Conclusions about GTL

- GTL arbitrary-angle Booleans is near optimal
- Performance of GTL arbitrary-angle Booleans is middle-of-road for small inputs
- Performance of GTL arbitrary-angle Booleans is best in class for large inputs
- Performance of GTL could be improved by up to 10X with further work on the arbitrary-angle Booleans
- If you have 45-degree or Manhattan polygons gtl provides 50X and 100X performance advantage over cgal

# Observations on GPC, CGAL and PolyBoolean

- We found at least two different bugs in PolyBoolean
- We found one bug in CGAL
- GPC and PolyBoolean have very difficult to use C-style APIs
- GPC and PolyBoolean cannot merge multiple overlapping polygons in one step
- GPC and PolyBoolean both have  $O(n^{1.5} \log n)$  line segment intersection algorithms (sort all edges that intersect sweep-line at every  $x$ )
- PolyBoolean has  $O(n * m * k)$  algorithm to determine which polygons contain which holes ( $n$  polygons,  $m$  holes,  $k$  points per polygon), which is  $O(n^2)$  in the worst case
- CGAL requires that overlapping polygons be merged before being an input to a Boolean, but can do that itself

# Observations About Preconditions

- CGAL throws an “Precondition Violated” exception if an input polygon is self intersecting/overlapping or has “closed” semantic at last vertex
- PolyBoolean returns a “bad input polygon” error code if an input polygon is self intersecting/overlapping has zero area or is a hole with no enclosing polygon
- Both PolyBoolean and CGAL inform the user the input is bad when a bug in their algorithms leads to a fatal error
- GPC produces garbage output when input polygons are self intersecting/overlapping
- GTL has no preconditions and produces correct output in all cases

# Generic Sweep-line Algorithm

- Sweep-line algorithms for polygon clipping is a tradition that goes back to 1979
- Sweep-line is the best known method for line segment intersection
- GTL implements different sweep lines for Manhattan, 45-degree and general case
- GTL Booleans sweep-lines are parameterized to allow them to perform multiple operations

# Better Booleans through Calculus

- We use the same algorithm for Manhattan, 45-degree and general polygon Booleans

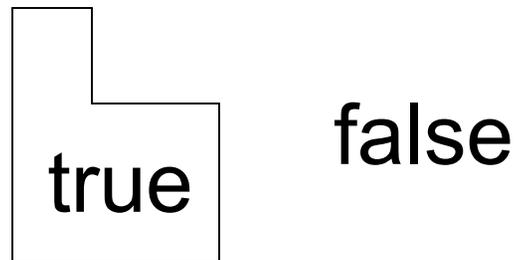
$$\frac{d}{dx} \frac{d}{dy} \text{ [Notch Polygon] } = \text{ [Vector Field] }$$

- We will explain how it works in the Manhattan case first, then how we generalize it

$$\int_{x=-\infty}^{\infty} \int_{y=-\infty}^{\infty} \text{ [Vector Field] } = \text{ [Notch Polygon] }$$

# Boolean Polygon Model

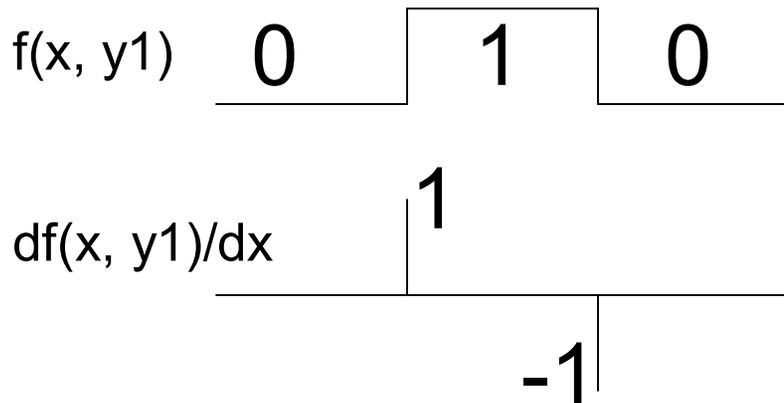
- We define a polygon as a two dimensional Boolean function
  - Function evaluates to true inside the polygon
  - Function evaluates to false outside the polygon



$$\text{inside\_polygon} = f(x, y)$$

# Math With Polygon Model

- Because the Polygon is now modeled mathematically...
- We can manipulate it with calculus
- The derivative with respect to x of the polygon function is the change in polygon count as we cross its vertical edges
- In one dimension the polygon looks like a step function at its vertical edges
- Derivative of a step function is an impulse with area of one
- Summing changes in polygon count from left to right (scanline) performs an integration over the  $df/dx$  to produce the original polygon



$$\int_{-\infty}^{\infty} \left( \begin{array}{c} | \\ 1 \\ | \end{array} \begin{array}{c} | \\ -1 \\ | \end{array} \right) dx = \text{[Polygon]}$$

$$\text{changing\_polygon\_count} = df(x, y)/dx$$

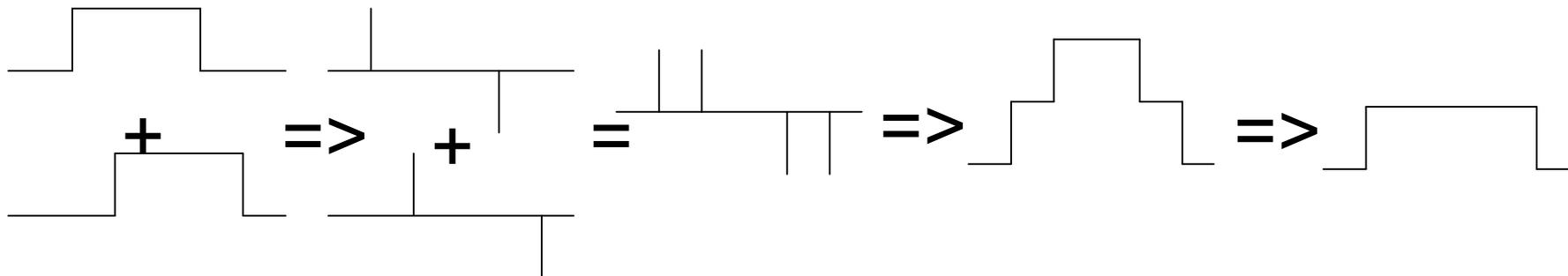
# The Great Thing About Math

- If it works once, it will work a second time
- The derivative with respect to y of the d/dx of polygon function f is the change in the change in polygon count with respect to x as we enter and leave its vertical edges in the y dimension
- In the y dimension d f/dx (vertical edges) looks like a step function
- Derivative of a step function is an impulse with area of one
- Summing changes in y of changes in x from low to high y integrates the function and produces changes in x (edges) that can be integrated left to right to produce polygons

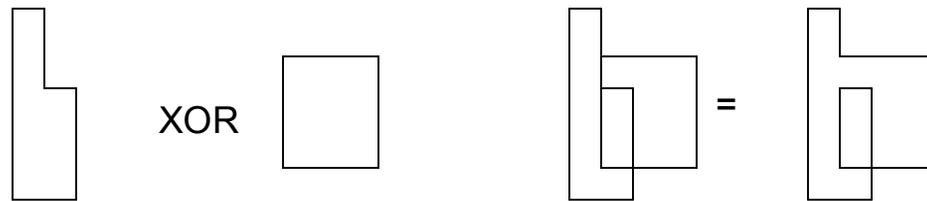
$$\begin{array}{c}
 f'(x, y) \quad \begin{array}{|c|c|c|} \hline 0 & 1 & 0 \\ \hline \end{array} \\
 \hline
 df'(x, y)/dy \quad \begin{array}{|c|c|c|} \hline & 1 & \\ \hline \end{array} \\
 \hline
 \text{change\_of\_change} = \begin{array}{|c|c|c|} \hline & -1 & \\ \hline \end{array}
 \end{array}
 \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \begin{array}{cc} \circ_{-1} & \circ_{+1} \\ \circ_{-1} & \circ_{+1} \\ \circ_{+1} & \circ_{-1} \end{array} dx dy = \begin{array}{|c|c|} \hline \square & \square \\ \hline \end{array}$$

# 1D Boolean OR Operation Example

- We want a data model for polygons that can provide the input for sweep-line and be constructed from  $n$  polygon vertices in  $O(n \log n)$  time
- If you want to sum two piece-wise linear functions (continuous)
  - you can take the derivative of each (discrete)
  - combine their derivatives in linear time by merging (sum any overlapping values)
  - and then integrate by summing from low to high (in linear time)
- The math is what allows the boolean algorithm to achieve optimal time complexity
  - All we do is sort vertices, but you have to carry the  $dx dy$  values along with them so that the meaning of the vertices is retained

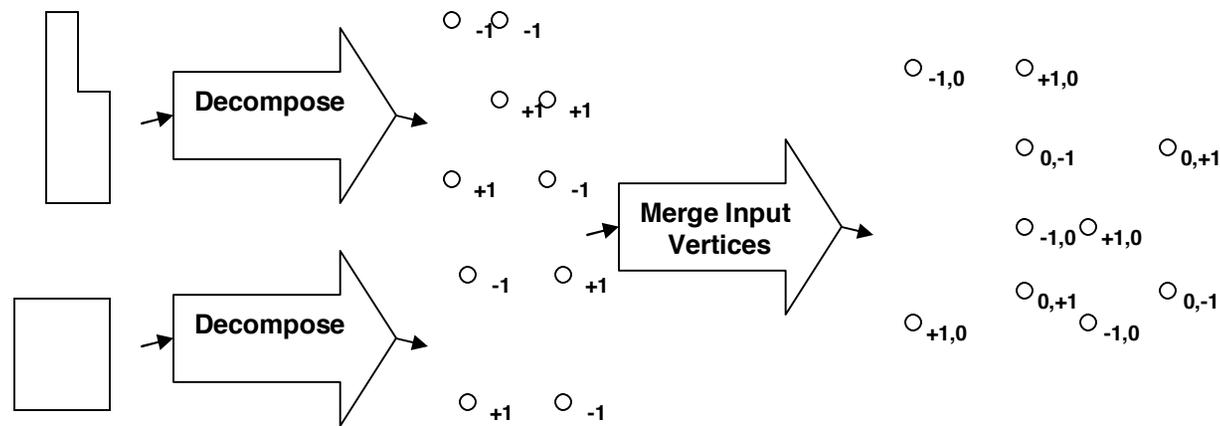


# 2D, Two Layer Boolean XOR Example



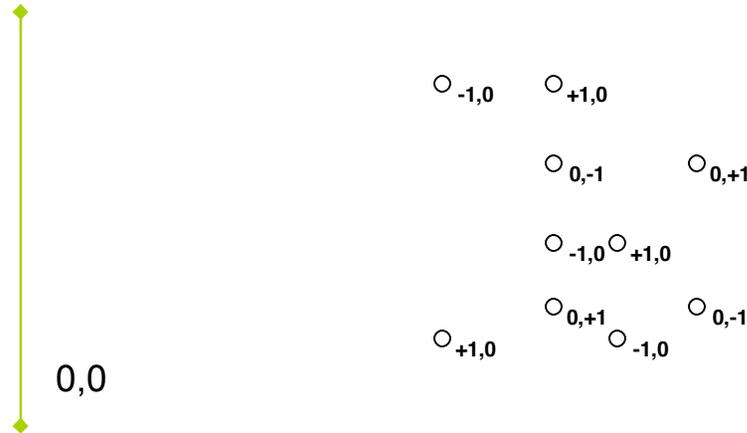
- XOR an L shape with a rectangle

# XOR Example



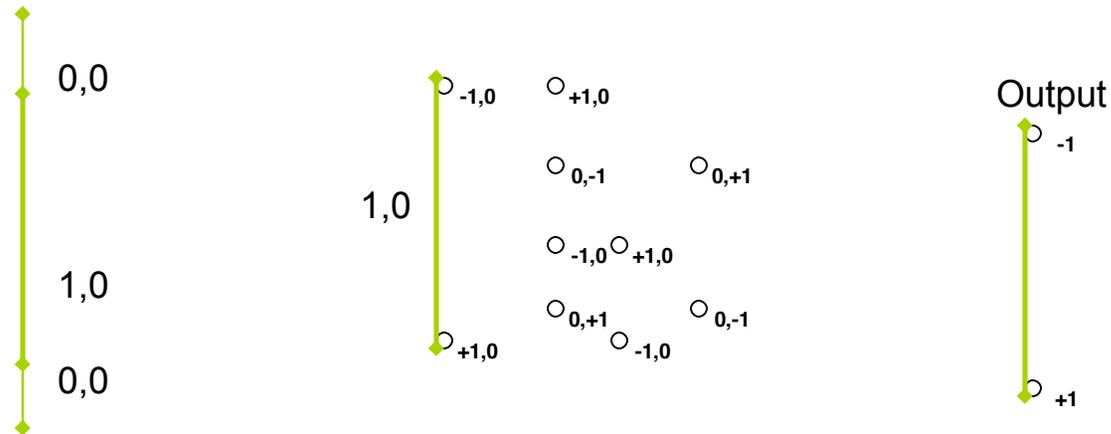
- Preprocess input polygons into a merged, sorted sequence of change on y of change on x of polygon intersection count
- Decomposition is linear, sort is  $n \log n$ , merge is linear

# XOR Example



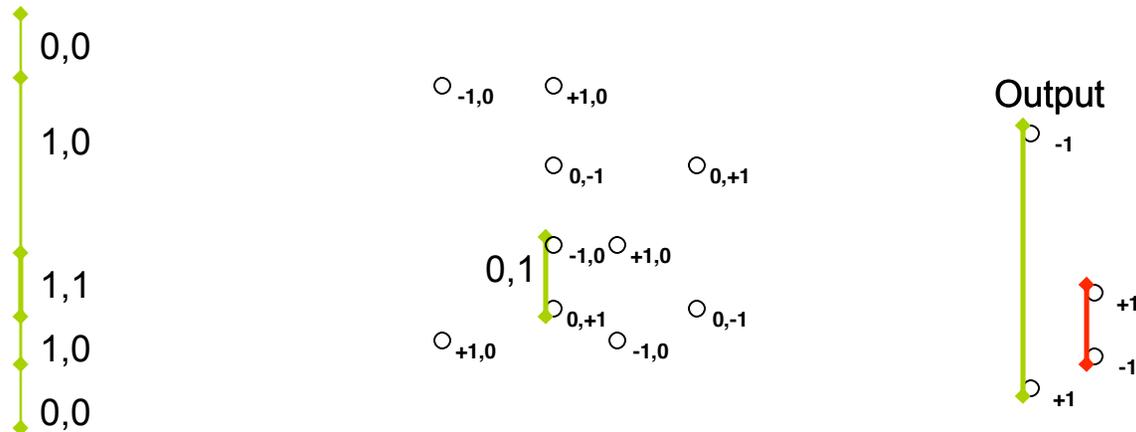
- Sweep-line data structure initialized to a single interval from  $-\infty$  to  $+\infty$  with intersection count of zero for each input layer

# XOR Example



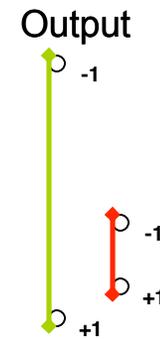
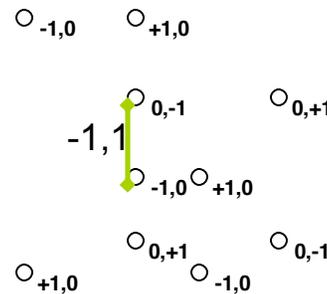
- Intersect first input interval of intersection count change on x against sweep-line data structure of intersection count intervals
- Intersection count changes from zero to one on layer1 on that interval
- $0 \text{ xor } 0 = \text{false}$ ,  $1 \text{ xor } 0 = \text{true}$ , output a left edge because Boolean logic changed from false to true

# XOR Example



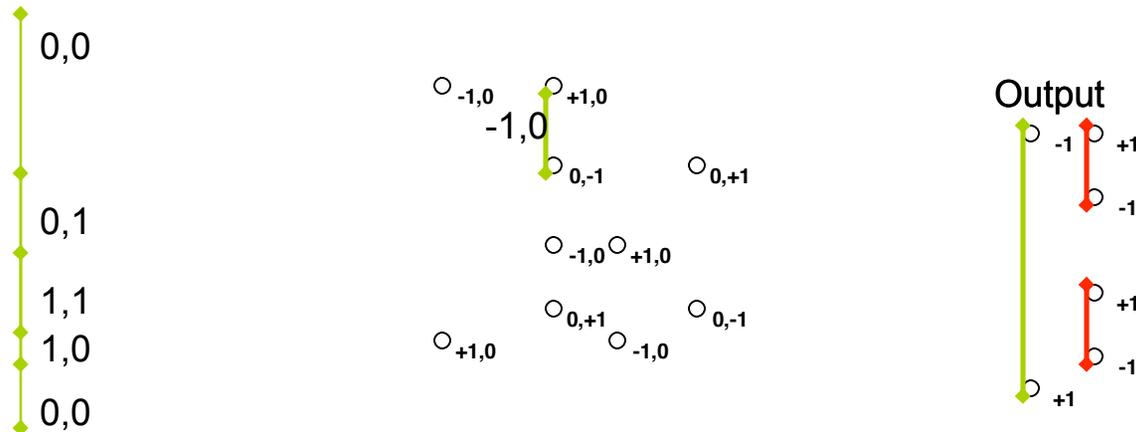
- Intersect second input interval against sweep-line data structure
- Intersection count changes from zero to one for layer2 on that interval
- $1 \text{ xor } 0 = \text{true}$ ,  $1 \text{ xor } 1 = \text{false}$ , so output a right edge because Boolean logic has changed from true to false

# XOR Example



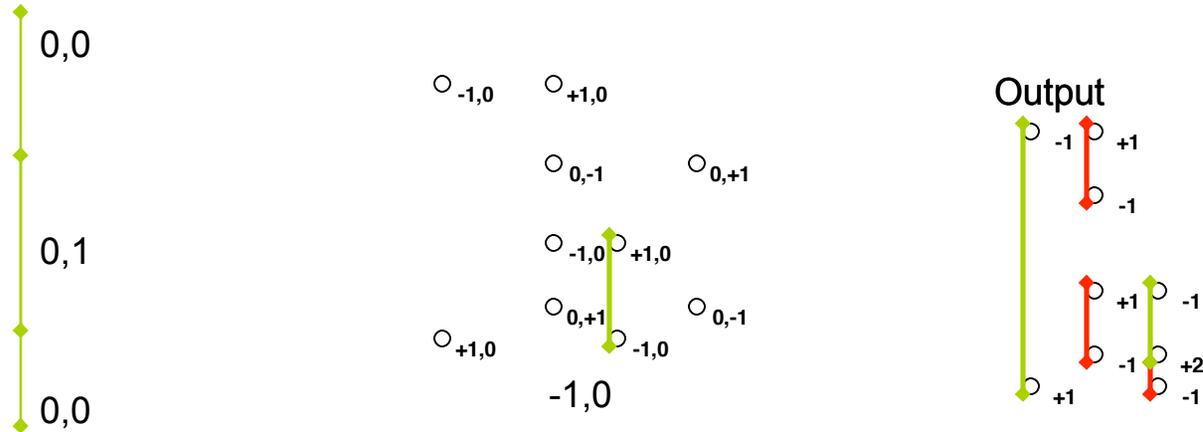
- Intersect third input interval against sweep-line data structure
- Intersection count changes from one to zero for layer1 on that interval
- $1 \text{ xor } 0 = \text{false}$ ,  $0 \text{ xor } 1 = \text{false}$ , so no output

# XOR Example



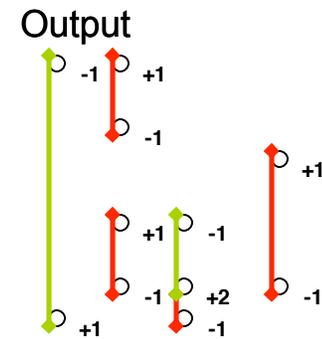
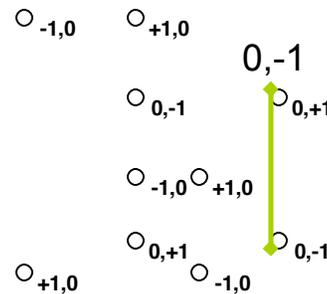
- Intersect fourth input interval against sweep-line data structure
- Intersection count changes from one to zero for layer1 on one interval
- $1 \text{ xor } 0 = \text{true}$ ,  $0 \text{ xor } 0 = \text{false}$ , so output a right edge because Boolean logic has changed from true to false

# XOR Example



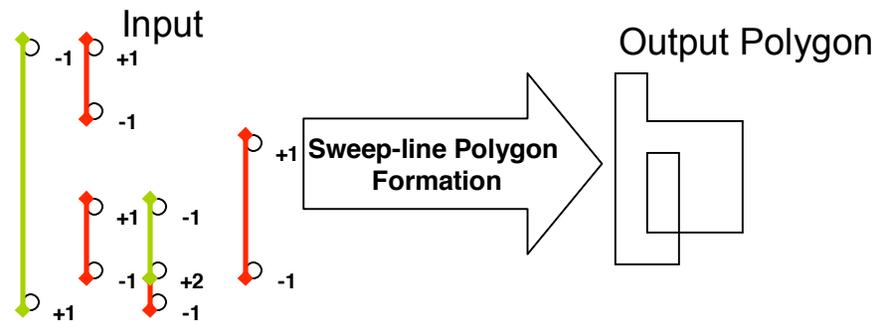
- Intersect fifth input interval against sweep-line data structure
- Intersection count changes from one to zero for layer1 on two intervals
- $1 \text{ xor } 0 = \text{true}$ ,  $0 \text{ xor } 0 = \text{false}$ , so output a right edge for the first interval
- $1 \text{ xor } 1 = \text{false}$ ,  $0 \text{ xor } 1 = \text{true}$ , so output a left edge for the second interval

# XOR Example



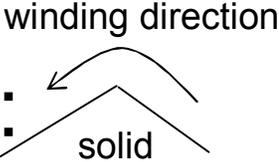
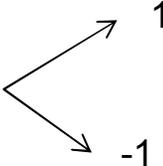
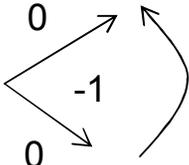
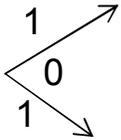
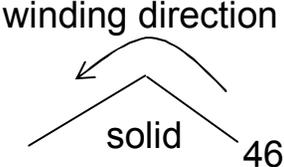
- Intersect sixth input interval against sweep-line data structure
- Intersection count changes from one to zero for layer2 on one interval
- $0 \text{ xor } 1 = \text{true}$ ,  $0 \text{ xor } 0 = \text{false}$ , so output a right edge

# XOR Example



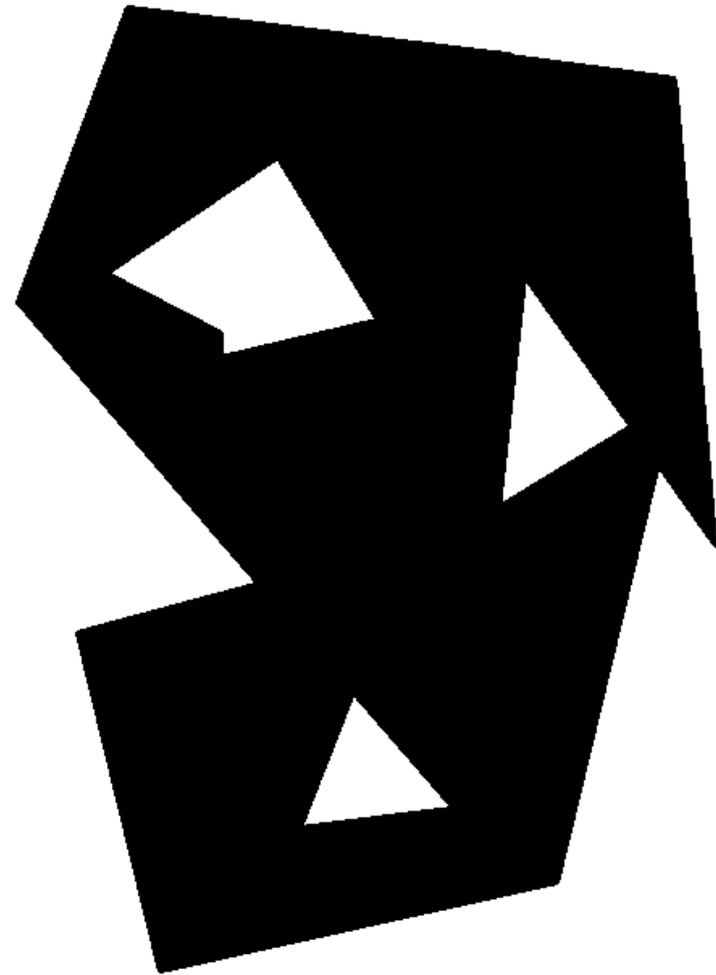
- Sweep-line Polygon Formation produces output polygon
- Could be done in the same pass as the xor
- Leaving it in the derivative form allows direct input to a subsequent Boolean

# Generalizing The Algorithm

- We want the derivative of this vertex: 
- We apply  $d/dx$  and  $d/dy$
- To get a result in terms of  $\theta$ : 
- We sweep the  $\theta$  from low to high: 
- As we integrate wrt.  $y$ : 
- And finally integrate wrt.  $x$ : 
- To which we assign counter clockwise winding and output partial polygon: 

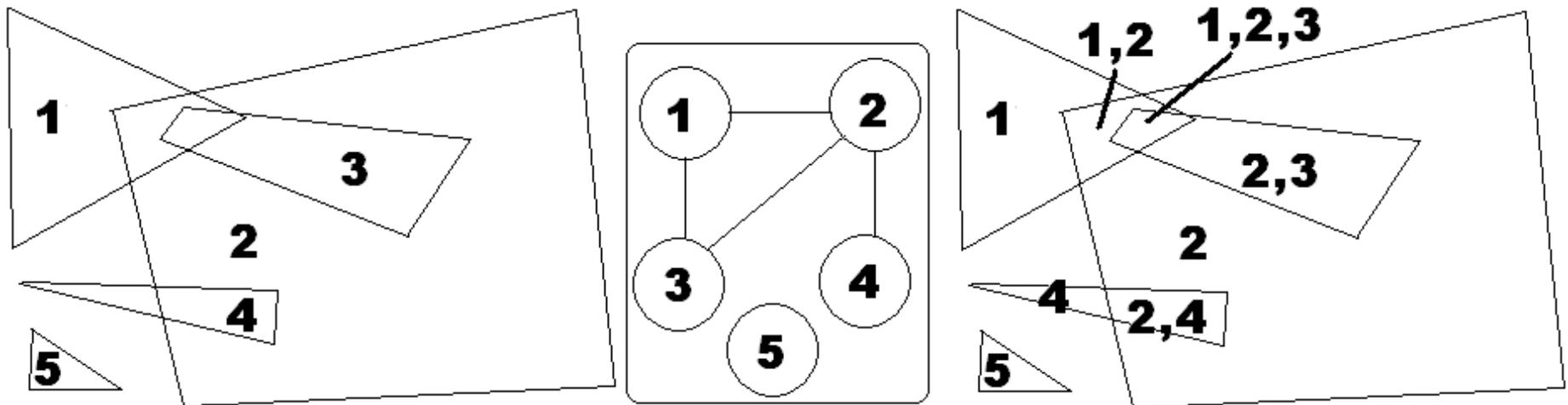
# The Algorithm Requires No Preconditions

- The great thing about math is that it's general
- Every special case is just another instance of the general case
- Every case that breaks other algorithms is handled implicitly and correctly



# Taking Things One Step Further

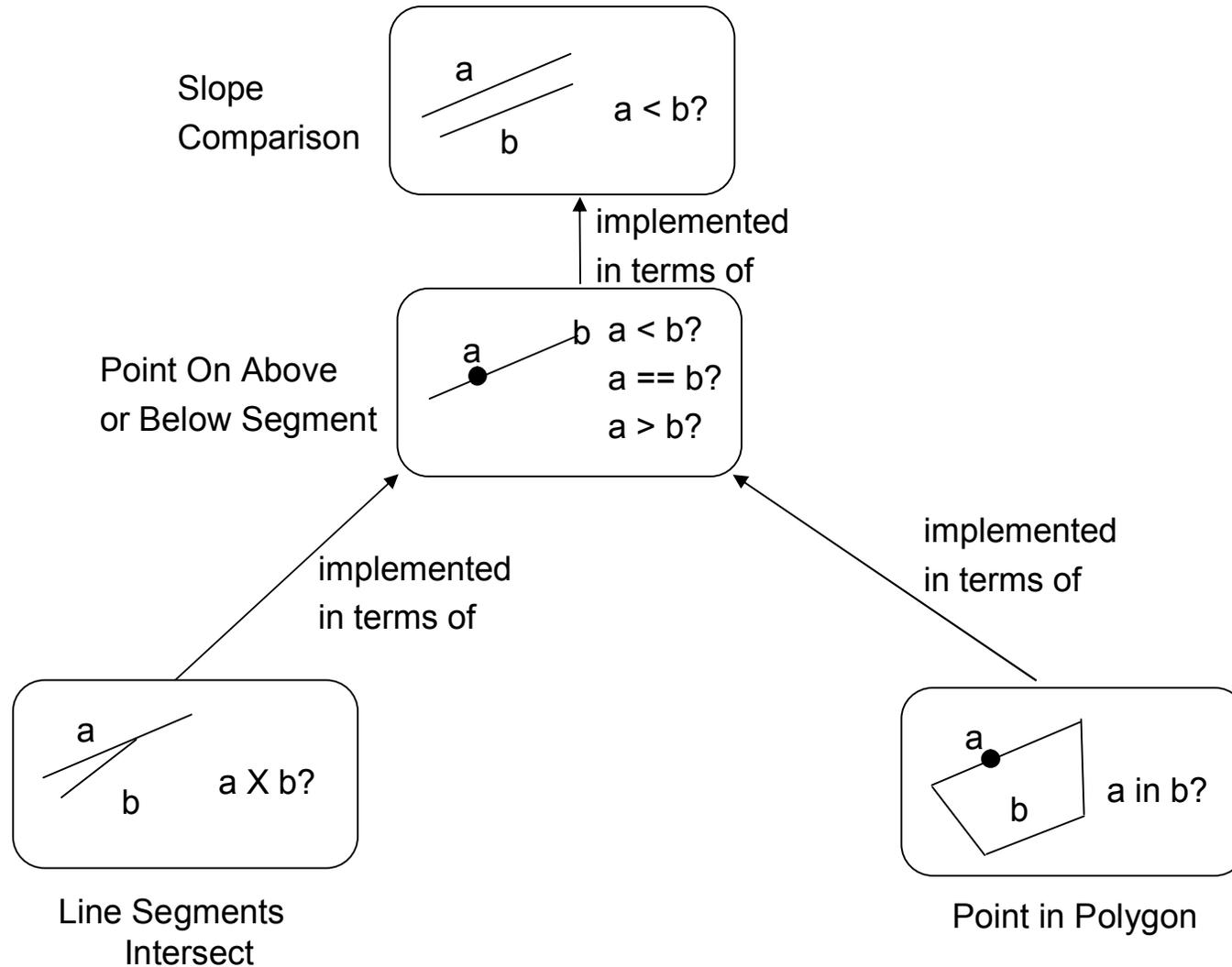
- The Booleans algorithm is parameterized
- N layer operations are implemented with a single pass of the same algorithm
- Is used to provide connectivity extraction / spatial map join and property merge / map overlay



# Robustness

- Strategies employed by GTL are provably robust for all cases
  - 100% robust--not just “works for all the cases we’ve tried”
- A firm guarantee of 100% numerical robustness is a very comforting feature
- PolyBoolean fails to find polygons that enclose some holes because its point-in-polygon calculation is not numerically robust

# Robust Predicate Primitives



# Robust Comparison of Slope

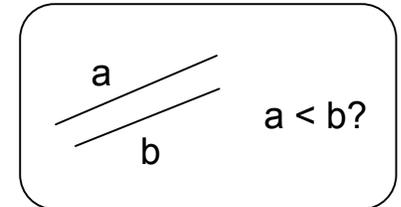
Segment 1:  $(x_{11}, y_{11})$  to  $(x_{12}, y_{12})$

Segment 2:  $(x_{21}, y_{21})$  to  $(x_{22}, y_{22})$

Slope1:  $(y_{12} - y_{11}) / (x_{12} - x_{11})$

Slope2:  $(y_{22} - y_{21}) / (x_{22} - x_{21})$

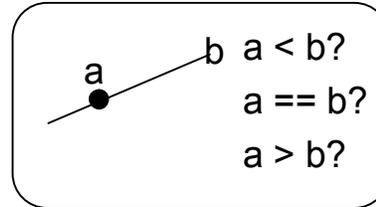
Slope1 < Slope2 iff  $(y_{12} - y_{11})(x_{22} - x_{21}) < (x_{12} - x_{11})(y_{22} - y_{21})$



- Cross multiplication avoids integer truncation of division
- Requires 65 bits for signed 32 bit integer coordinates
  - Use long double, multi-precision, SSE quad word, or unsigned 64 bit integer with sign computed separately

# Robust Comparison Of Point and Line Segment

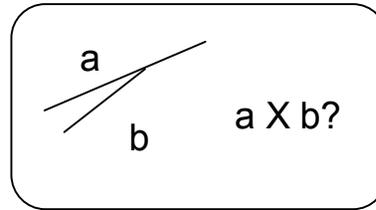
Point On Above  
or Below Segment



- Make a 2<sup>nd</sup> segment from one end of the segment to the point
- Compare slopes

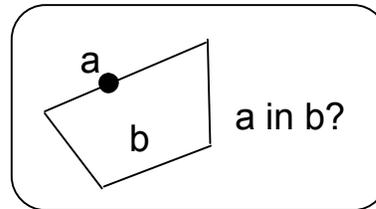


# Robust Line Segment Intersection Check



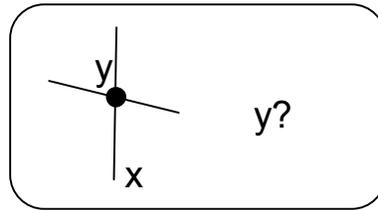
- Compute whether the two ends of each segment are on, above or below the other segment
- Both points of one segment on the same side of the other means no intersection

# Robust Point In Polygon Predicate



- For all edges which contain the x value of the point within their x interval
  - Accumulate the sum of such edges the point is above
- The point is inside if the sum is odd

# Robust Calculation of Slope Intercept



- Apply GMP multi-precision rational and compute exact result
- To compare two slope intercepts

```
//Segment 1: (x11,y11) to (x12, y12)
```

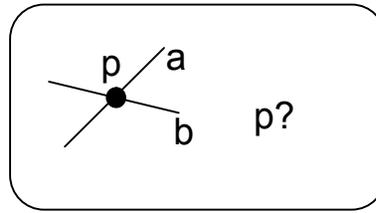
```
//Segment 2: (x21,y21) to (x22, y22)
```

```
y1 < y2 iff
```

$$(x_{22} - x_{21})((x - x_{11})(y_{12} - y_{11}) + y_{11}(x_{12} - x_{11})) < (x_{12} - x_{11})((x - x_{21})(y_{22} - y_{21}) + y_{21}(x_{22} - x_{21}))$$

(requires 97 bits of precision)

# Robust Calculation of Line Segment Intersection Point

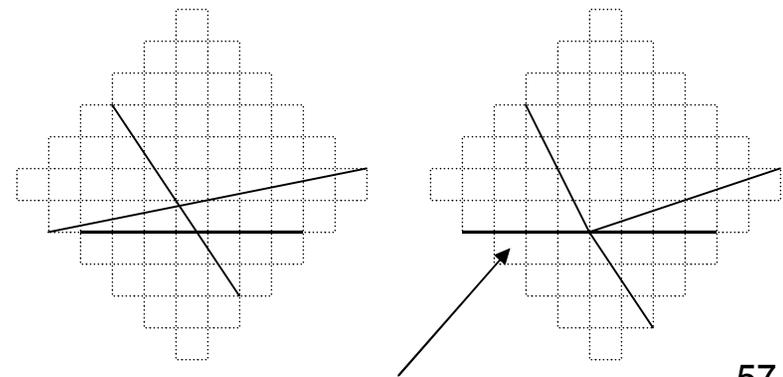
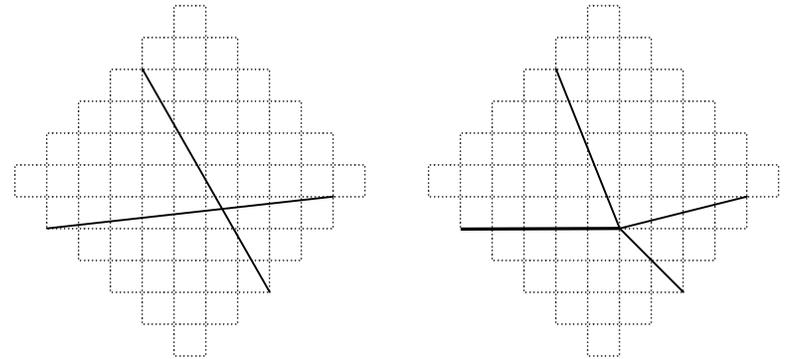


- Apply GMP multi-precision rational and compute exact result.

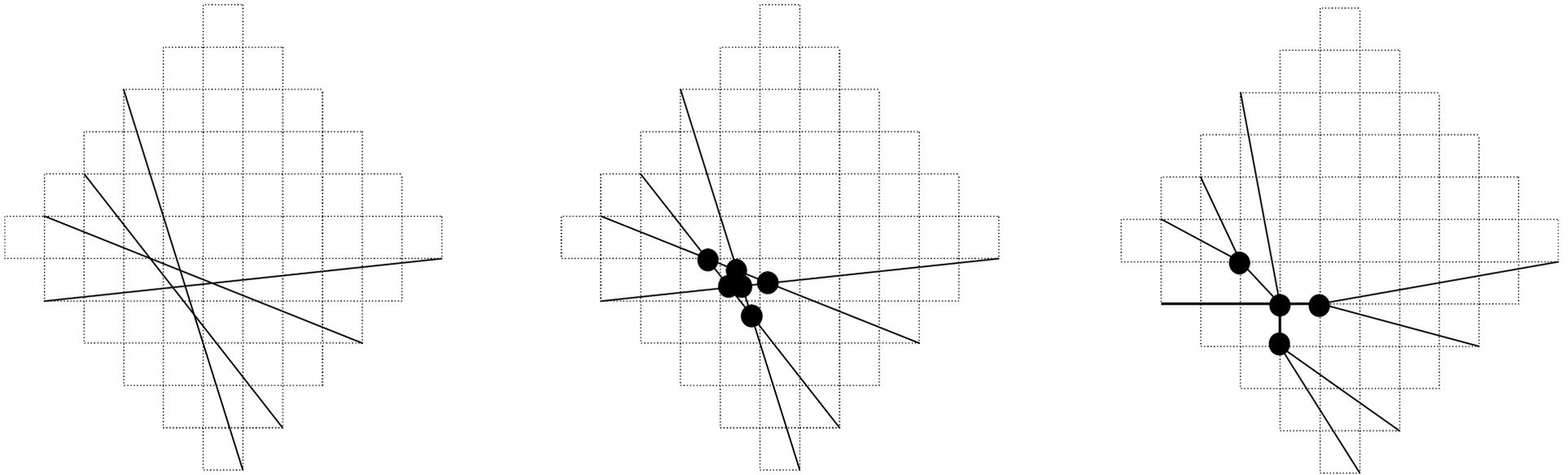
```
//Segment 1: (x11,y11) to (x12, y12)
dx1 = x12 - x11;  dy1 = y12 - y11;
//Segment 2: (x21,y21) to (x22, y22)
dx2 = x22 - x21;  dy2 = y22 - y21;
x = (x11 * dy1 * dx2 - x21 * dy2 * dx1 +
     y21 * dx1 * dx2 - y11 * dx1 * dx2) /
   (dy1 * dx2 - dy2 * dx1);
y = (y11 * dx1 * dy2 - y21 * dx2 * dy1 +
     x21 * dy1 * dy2 - x11 * dy1 * dy2) /
   (dx1 * dy2 - dx2 * dy1);
```

# Robust Snapping of Non-Integer Intersection Points to Grid

- Truncate down and to left
- Causes Edges to move slightly
- Moving edges may introduce artifacts
- Non overlapping edges may become parallel and overlap



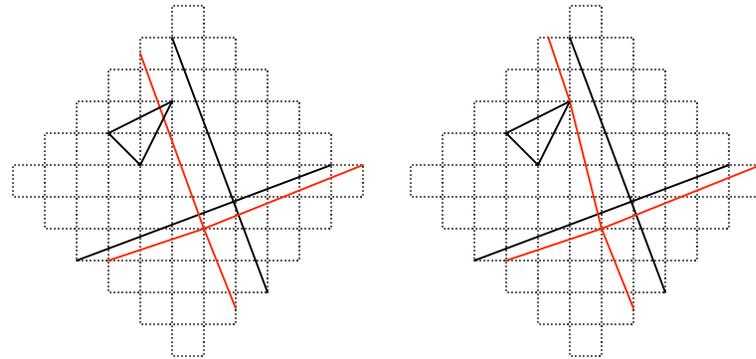
# Intersection Clusters



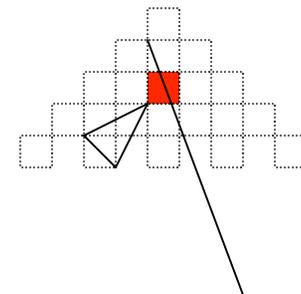
- Multiple intersection points within the same unit grid are merged

# Intersections Creating Intersections

- When long edges are moved by integer truncation of intersection point
- Very close geometry may be intersected
- Intersect segments with very close vertices



- Sufficient to check the upper right grid for line segments



# Acceptable vs. Unacceptable Artifacts

- An artifact is unacceptable
  - if it causes any line segments to intersect other than at their end points
  - if it causes a closed cycle in the input to become open at the output
- Inserting vertices on line segments and merging vertices are acceptable
- We insert vertices and merge vertices to snap to integer grid robustly

# What code that uses GTL looks like

```
void foo(list<CPolygon>& result,
        const list<CPolygon>& a,
        const list<CPolygon>& b) {
    CBoundingBox domainExtent;
    gtl::extents(domainExtent, a);
    result += (b & domainExtent) ^ (a - 10);
}
```

- Two lines of code in the example invoke five different GTL algorithms
- Arguments passed into functions are not GTL data types
- The code is maximally concise, yet easy to read
- Clip `b` to the bounding box of `a`, XOR that with `a` shrunk by ten then merge into `result`
- Details of memory management for intermediate results are abstracted away from the use of algorithms
- Such code is easy to write and easy to maintain

# C++ Concepts-based Type System

- GTL allows application data types to be arguments to its API
- You can check if your point type lies inside your polygon type with a call to GTL `contains()` passing in your point and your polygon

```
    gtl::contains(my_polygon, my_point);
```
- This is accomplished by use of a C++ Concepts-based statically polymorphic type system
- This is much more convenient than copying your polygon into a GTL polygon data type first

# C++ Traits

- GTL accesses your geometry types through type traits that you must provide
- These traits map your implementation of a geometry object to GTL's concept of how a such geometry behaves

```
template <typename T>
struct point_traits {
typedef T::coordinate_type coordinate_type;
coordinate_type get(const T& p, orientation_2d orient) {
    return p.get(orient);
}
}
template <typename T>
struct point_mutable_traits {
    void set(const T& p, orientation_2d orient,
            coordinate_type value) {
        p.set(orient, value);
    }
    T construct(coordinate_type x, coordinate_type y) {
        return T(x, y); }
};
```

# C++ Concepts Overloading

- GTL functions that expect a polygon check whether the input data type is registered as a polygon and will not instantiate if the check fails
- A different gtl function with the same name can instantiate if the data type turns out to be registered as a rectangle, or a point
- The mechanism for doing this is called substitution failure is not an error (SFINAE)

```
template <typename T> struct is_integer {};  
template <>  
struct is_integer<int> { typedef int type; };  
template <typename T> struct is_float {};  
template <>  
struct is_float<float> { typedef float type; };  
  
template <typename T>  
typename is_int<T>::type foo(T input);  
template <typename T>  
typename is_float<T>::type foo(T input);
```

foo() would be ambiguous, but both return types cannot be instantiated with the same type. Failure to instantiate the return type is not a syntax error.

# Concept Refinement

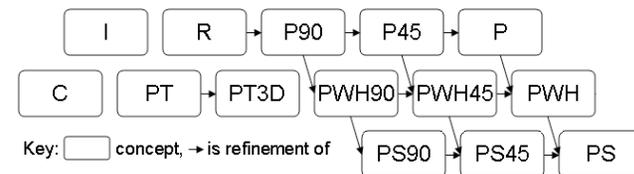
- A rectangle is a refinement of the concept of a polygon
  - A rectangle narrows-down the definition of polygon to four sided, 90-degree angles
- A function that requires read only access to a polygon can always work on a rectangle
  - A polygon is a generalization of a rectangle
- A function that requires write-access to a polygon cannot work on a rectangle
  - A rectangle cannot store a polygon

```
struct polygon_concept {};  
struct rectangle_concept {};  
template <typename T>  
struct is_a_polygon_concept{};  
template <> struct is_a_polygon_concept<rectangle_concept> {  
    typedef gtl_yes type; };
```

# GTL Refinement Relationships

- GTL assign() function
  - copies data between objects of the same conceptual type
  - copies data from a refinement to a more general conceptual type
  - instantiates for each of the 49 legal combinations
  - requires only one overload definition per concept type
  - each overload protected by SFINAE concept check

Concept	Abbreviation
coordinate_concept	C
interval_concept	I
point_concept	PT
point_3d_concept	PT3D
rectangle_concept	R
polygon_90_concept	P90
polygon_90_with_holes_concept	PWH90
polygon_45_concept	P45
polygon_45_with_holes_concept	PWH45
polygon_concept	P
polygon_with_holes_concept	PWH
polygon_90_set_concept	PS90
polygon_45_set_concept	PS45
polygon_set_concept	PS



# Concept Casting

- A Manhattan polygon is a refinement of a general polygon
- Given a general polygon and the certainty that it contains only Manhattan data
  - GTL `view_as<polygon_90_concept>()` can allow that polygon to be legally passed to functions expecting a Manhattan polygon
- This is useful when general objects are used by applications to model several specific kinds of data

# Booleans Operator Syntax

- GTL overloads the C++ bit-wise logical operators  $\&$ | $^$  and the subtraction operator -
- They perform Boolean AND, OR, XOR and AND-NOT (SUBTRACT)
- They work with any polygons, rectangles, vectors or lists of polygons or rectangles and the GTL polygon-set data types

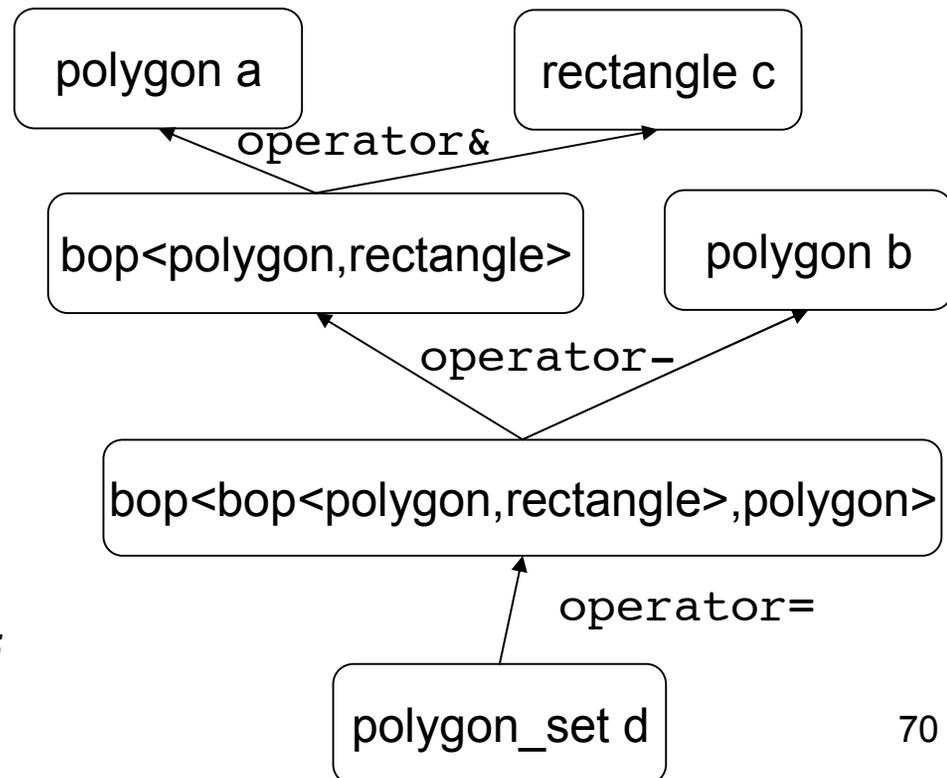
# GTL Booleans Operator Templates

- C++ requires that operators return their result by value
- The return value of a GTL Boolean operator function call is an operator template
- The operator template stores references to the arguments and defers the operation until the result is requested
- In this way the operation is performed after the operator template is returned by the operator function

# Operator Templates

```
void clip_and_subtract(polygon_set& d,  
                      polygon a, polygon b, rectangle c) {  
    d = (a & c) - b;  
}
```

- When chaining operator templates they cache references to each other and build an expression tree
- When the final result is requested the expression is evaluated and the result is produced
- This avoids unnecessary copying of intermediate results



# MSVC SFINAE limitation

- SFINAE works in MSVC for the simple cases
- Order of template instantiation in MSVC depends on type of template
  - compile time constant vs. by type
- Substitution failure of a nested template is an error in MSVC
- The only way to get reliable SFINAE behavior out of MSVC is to use `enable_if` with compile time logic expressions
- It took two weeks of work to port the code from EDG/gcc compatibility to MSVC

# EDG SFINAE Bug

- An unnamed enum type cannot be referred to in the template definition when instantiating a template on that type
- STL uses unnamed enum types with arithmetic operators
- Substitution of my generic operators for the unnamed STL enum types should fail
- A bug in older versions of EDG frontend produces a syntax error instead of SFINAE if the template references it in the definition
- Currently fixed in the version of EGD used by the new icc11

# EDG Bug Workaround

- If substitution of a nested template parameter fails before EDG tries to instantiate the template that would refer to the unnamed enum type no syntax error is generated
- EDG supports nested SFINAE, of course
- I provide an intermediate meta-function with preprocessor macros in its definition that results in nested SFINAE except when compiled by MSVC to work around both bugs

```
template <typename T> struct gtl_if {  
#ifdef WIN32  
    typedef gtl_no type;  
#endif  
};  
template <> struct gtl_if<gtl_yes> { typedef gtl_yes type; };
```